

THE EVOLVING INTERSTELLAR MEDIUM OF STAR-FORMING GALAXIES SINCE $z = 2$ AS PROBED BY THEIR INFRARED SPECTRAL ENERGY DISTRIBUTIONS

GEORGIOS E. MAGDIS¹, E. DADDI², M. BÉTHÉMIN², M. SARGENT², D. ELBAZ², M. PANNELLA², M. DICKINSON³,
 H. DANNERBAUER⁴, E. DA CUNHA⁵, F. WALTER⁵, D. RIGOPOULOU^{1,6}, V. CHARMANDARIS^{7,8,9},
 H. S. HWANG¹⁰, AND J. KARTALTEPE³

¹ Department of Physics, University of Oxford, Keble Road, Oxford OX1 3RH, UK

² CEA, Laboratoire AIM, Irfu/SAP, F-91191 Gif-sur-Yvette, France

³ NOAO, 950 N. Cherry Avenue, Tucson, AZ 85719, USA

⁴ Institut für Astronomie, Universität Wien, Türkenschanzstrasse 17, A-1180 Wien, Austria

⁵ Max-Planck-Institut für Astronomie, Königstuhl 17, D-69117 Heidelberg, Germany

⁶ Space Science & Technology Department, Rutherford Appleton Laboratory, Chilton, Didcot, Oxfordshire OX11 0QX, UK

⁷ Department of Physics & ICTP, University of Crete, GR-71003, Heraklion, Greece

⁸ IESL/Foundation for Research & Technology-Hellas, GR-71110, Heraklion, Greece

⁹ Chercheur Associé, Observatoire de Paris, F-75014 Paris, France

¹⁰ Smithsonian Astrophysical Observatory, 60 Garden Street, Cambridge, MA 02138, USA

Received 2012 July 17; accepted 2012 September 21; published 2012 October 29

ABSTRACT

Using data from the mid-infrared to millimeter wavelengths for individual galaxies and for stacked ensembles at $0.5 < z < 2$, we derive robust estimates of dust masses (M_{dust}) for main-sequence (MS) galaxies, which obey a tight correlation between star formation rate (SFR) and stellar mass (M_*), and for starbursting galaxies that fall outside that relation. Exploiting the correlation of gas-to-dust mass with metallicity ($M_{\text{gas}}/M_{\text{dust}}-Z$), we use our measurements to constrain the gas content, CO-to-H₂ conversion factors (α_{CO}), and star formation efficiencies (SFE) of these distant galaxies. Using large statistical samples, we confirm that α_{CO} and SFE are an order of magnitude higher and lower, respectively, in MS galaxies at high redshifts compared to the values of local galaxies with equivalently high infrared luminosities ($L_{\text{IR}} > 10^{12} L_{\odot}$). For galaxies within the MS, we show that the variations of specific star formation rates (sSFRs = SFR/M_*) are driven by varying gas fractions. For relatively massive galaxies like those in our samples, we show that the hardness of the radiation field, $\langle U \rangle$, which is proportional to the dust-mass-weighted luminosity ($L_{\text{IR}}/M_{\text{dust}}$) and the primary parameter defining the shape of the IR spectral energy distribution (SED), is equivalent to SFE/ Z . For MS galaxies with stellar mass $\log(M_*/M_{\odot}) \geq 9.7$ we measure this quantity, $\langle U \rangle$, showing that it does not depend significantly on either the stellar mass or the sSFR. This is explained as a simple consequence of the existing correlations between $\text{SFR}-M_*$, M_*-Z , and $M_{\text{gas}}-\text{SFR}$. Instead, we show that $\langle U \rangle$ (or equally $L_{\text{IR}}/M_{\text{dust}}$) does evolve, with MS galaxies having harder radiation fields and thus warmer temperatures as redshift increases from $z = 0$ to 2, a trend that can also be understood based on the redshift evolution of the M_*-Z and $\text{SFR}-M_*$ relations. These results motivate the construction of a universal set of SED templates for MS galaxies that are independent of their sSFR or M_* but vary as a function of redshift with only one parameter, $\langle U \rangle$.

Key word: galaxies: evolution

Online-only material: color figures

1. INTRODUCTION

Deep and wide multi-wavelength extragalactic surveys have greatly enhanced our understanding of galaxy evolution. It has now been well established that the star formation rates (SFRs) in galaxies were on average higher in the past, with galaxies emitting the bulk of their bolometric energy in the infrared (IR) progressively dominating the star formation density of the universe that peaked at $z \geq 1$ (e.g., Le Borgne et al. 2009).

A recent major step forward in characterizing the nature of star formation in distant galaxies has been the discovery that the majority of star-forming galaxies at every redshift define a narrow locus in the stellar mass (M_*)-SFR plane. This correlation has been observed in the local universe (Brinchmann et al. 2004; Peng et al. 2010), as well as at intermediate redshifts $0.5 < z < 3$ (Noeske et al. 2007; Elbaz et al. 2007; Daddi et al. 2007; Pannella et al. 2009; Rodighiero et al. 2010; Karim et al. 2011; Magdis et al. 2010b), and beyond (e.g., Daddi et al. 2009; Stark et al. 2010), with a normalization factor that increases

rapidly with look-back time, mirroring the increase in the star formation activity of the early galaxies.

The fact that this correlation between SFR and M_* appears to be present at all epochs has been used to define a characteristic specific star formation rate (sSFR $\equiv \text{SFR}/M_*$) at each redshift and stellar mass and, from its evolution with cosmic time, a main-sequence (MS) mode of star formation that is followed by the majority of star-forming galaxies. This MS also serves as a tool to distinguish starburst (SB) from normal¹¹ galaxies at any redshift, simply by measuring the excess sSFR of the galaxy with respect to the $\text{SFR}-M_*$ correlation at that redshift. Such outliers are known to exist at any redshift. In the local universe, a class of galaxies that are usually identified as SBs are the (ultra)luminous infrared galaxies (ULIRGs, $L_{\text{IR}} > 10^{12} L_{\odot}$; Sanders & Mirabel 1996; Elbaz et al. 2007). However, in the distant universe it has proven to be harder than initially thought

¹¹ Throughout the paper we will use the terms “normal” and “main-sequence” galaxy interchangeably.

to associate pure SBs with a specific class of high- z galaxies, although at least a fraction of submillimeter galaxies (SMGs) seem to exhibit elevated sSFRs (Tacconi et al. 2006, 2008; Daddi et al. 2007, 2009; Takagi et al. 2008).

The remarkable uniformity of MS galaxies, as indicated by the SFR- M_* correlation and their contrasting nature to that of SB galaxies, has recently been further manifested with respect to two more sets of observable parameters. Using direct measurements of the total infrared luminosity ($L_{\text{IR}} = L_{8-1000\mu\text{m}}$) of distant galaxies that have now become possible with the *Herschel Space Observatory* (Pilbratt et al. 2010), Elbaz et al. (2011) showed that galaxies that follow the SFR- M_* correlation are also part of a secondary, infrared MS, defined by a universal total-to-mid-IR luminosity ratio, $\text{IR8} \equiv L_{\text{IR}}/L_8$, where L_8 is the rest-frame $8\mu\text{m}$ luminosity. The majority of MS galaxies, at all luminosities and redshifts, are found to obey this linear correlation between L_{IR} and L_8 , suggesting that they share a common IR spectral energy distribution (SED), with a mid- to far-IR shape that has evolved little with cosmic time. Interestingly, SB galaxies, which systematically fall above the SFR- M_* MS, are also outliers to the $L_{\text{IR}}-L_8$ relation, exhibiting elevated IR8 values with respect to normal galaxies.

The third quantity that highlights the distinct nature of MS galaxies and SBs encompasses the main driver of star formation activity: the molecular gas mass (M_{H_2}), i.e., the raw material out of which galaxies form stars. Recent studies, by Daddi et al. (2010a) and Genzel et al. (2010), found that normal galaxies at any redshift have lower star formation efficiencies (SFE $\equiv \text{SFR}/M_{\text{H}_2}$) compared to starbursting systems that exhibit an accelerated mode of star formation activity, probably triggered by a major merger. These studies all suggest that there are two regimes of star formation: (1) a long-lasting mode, followed by the majority of galaxies at every redshift that also form a tight MS in the SFR- M_* and in the $L_{\text{IR}}-L_8$ planes, and (2) a short-lived SB mode for galaxies that can become strong outliers from both relations. However, this picture heavily relies on M_{H_2} estimates, which are still a matter of significant debate due to the poorly determined conversion factor to derive molecular gas mass from CO luminosities ($\alpha_{\text{CO}} = M_{\text{H}_2}/L'_{\text{CO}}$), which is known to vary as a function of metallicity and, perhaps, of the intensity of the radiation field (e.g., Leroy et al. 2011; Magdis et al. 2011).

Although the separation between SBs and MS galaxies is already apparent in the observed $L_{\text{IR}}-L'_{\text{CO}}$ plane, the distinct nature of the star formation activity of the two populations becomes truly evident when different α_{CO} factors are used for the two classes of galaxies. This differentiation of the α_{CO} value has clearly been seen in the nearby universe, with local ULIRGs (SBs) having a value of α_{CO} that is a factor of ~ 6 smaller than that for local spiral galaxies¹² (e.g., Downes & Solomon 1998), and seems to be true at high redshift too. Using a dynamical and a dust-to-gas mass ratio analysis of star-forming disks at $z \sim 1.5$, Daddi et al. (2010a) and Magdis et al. (2011) argued for a CO conversion factor¹³ $\alpha_{\text{CO}} \sim 4.0$ for this kind of object, similar to that of the Milky Way (MW) and local spirals. On the other hand, several studies place an upper limit of $\alpha_{\text{CO}} \sim 0.8$ for several SMGs (e.g., Tacconi et al. 2008; Carilli et al. 2010; Magdis et al. 2011; Hodge et al. 2012). Furthermore, recent

numerical simulations indicate a clear distinction between the α_{CO} values for disks and mergers at all redshifts, although with a considerable scatter (e.g., Narayanan et al. 2011; Feldmann et al. 2012). These findings challenge the common approach of “blindly” applying a (local) ULIRG-like $\alpha_{\text{CO}} = 0.8$ value to derive the M_{H_2} of high- z ULIRGs. Instead, they highlight the necessity of determining α_{CO} in larger samples of high- z galaxies and of investigating how it varies between normal galaxies and mergers/SB, but also among galaxies on the MS.

To this end, in Magdis et al. (2011) we applied, for the first time at high redshift, a method for measuring α_{CO} that is commonly used in the local universe. The method relies on measuring the total dust mass of a galaxy (M_{dust}) and assuming that it is proportional to M_{gas} (e.g., Leroy et al. 2011). Taking advantage of the detailed characterization of the peak of the SED enabled by *Herschel* data, as well as of the Rayleigh-Jeans tail from ground-based millimeter observations, we acquired robust M_{dust} estimates for a normal disk at $z \sim 1.5$ and a starbursting SMG at $z = 4.05$. The dust mass estimates were subsequently used to infer an α_{CO} value of ~ 4.0 for the disk and an upper limit of ~ 1 for the SB galaxy, in agreement with previous dynamical estimates (Daddi et al. 2010a; Hodge et al. 2012). This study also offered a first hint of a close link between the SED shape, as traced by the dust-weighted luminosity ($L_{\text{IR}}/M_{\text{dust}}$), and α_{CO} and SFE, with MS galaxies exhibiting lower $L_{\text{IR}}/M_{\text{dust}}$ values compared to SB galaxies.

Having demonstrated the applicability of the method at high redshift, here we extend this exercise to a larger sample of MS disks at $z \sim 1.5$ and $z \sim 0.5$ that have extensive photometry from rest-frame UV to millimeter wavelengths, including state-of-the-art *Herschel* data from the *Herschel* Great Observatories Origins Deep Survey (GOODS-*Herschel*, PI: D. Elbaz), as well as low-transition CO observations and millimeter continuum interferometric measurements. We use this to investigate the average α_{CO} value for high- z MS galaxies, finding consistent values with what is predicted by the local α_{CO} versus Z trend and what is inferred by dynamical analyses (Daddi et al. 2010b).

Pushing the method further, we here analyze large statistical samples of galaxies at $z \sim 1$ and $z \sim 2$ to derive their average dust and gas mass content. While the lack of CO measurements for such large samples prevents us from learning anything about their conversion factor, the recovered information is invaluable to study the distribution of gas in high-redshift galaxies. This allows us to investigate possible variations of gas fractions and SFE within the MS, providing insights about the origin of the “thickness” of the SFR- M_* relation that has been shown to reflect the variation of the physical properties of MS galaxies (e.g., Salmi et al. 2012; Elbaz et al. 2011). Furthermore, the available data allow us to investigate the SED shape of MS galaxies as a function of redshift and also as a function of their offset from the MS. Put together, in this study we attempt to characterize the gas, dust, and SED properties of MS galaxies throughout cosmic time and therefore provide a better understanding of the nature of the sources that dominate the star formation density at all redshifts (e.g., Rodighiero et al. 2011; Sargent et al. 2012).

This paper is organized as follows. In Section 2, we describe our sample and the multi-wavelength observations. In Section 3, we present a detailed analysis of the far-IR properties. In Section 4, we discuss the method to derive α_{CO} and present α_{CO} and SFE estimates for MS and SB galaxies. In Section 5, we explore the variations of SFE within the MS and discuss two possible scenarios to explain the observed dispersion of

¹² We note that Papadopoulos et al. (2012) presented evidence that higher α_{CO} values are possible in local ULIRGs.

¹³ The units of α_{CO} , $M_{\odot} \text{ pc}^{-2} (\text{K km s}^{-1})^{-1}$, are omitted from the text for brevity. Also, α_{CO} estimates in this work account for the presence of helium coexisting with the molecular hydrogen.

the $\text{SFR}-M_*$ correlation. In Section 6, we investigate these two scenarios through stacking, while in Section 7 we explore the shape of the SED of MS galaxies as a function of cosmic time and build template SEDs of MS galaxies in various redshift bins. Finally, in Section 8, we provide a discussion motivated by the results of this study, while a summary of the latter is presented in Section 9. Throughout the paper, we adopt $\Omega_m = 0.3$, $H_0 = 71 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_\Lambda = 0.7$, and a Chabrier initial mass function (IMF; Chabrier 2003).

2. OBSERVATIONS AND SAMPLE SELECTION

The aim of this study is to investigate the far-IR and gas properties of high- z , normal, MS galaxies. Instead of using a large, heterogeneous sample, we decided to focus on a small but well-defined set of sources selected to meet the following criteria: (1) available spectroscopic redshifts; (2) rich rest-frame UV to mid-IR photometry; (3) no excess in the sSFR , i.e., $\text{sSFR}/\text{sSFR}_{\text{MS}} < 3$ (where sSFR_{MS} is the MS trend, as detailed below); (4) available [1–0] or [2–1] low-transition CO observations, to enable CO luminosity estimates, without the caveat of the uncertainties introduced by the excitation corrections affecting higher CO transition lines; (5) *Herschel* detections that offer a detailed sampling of the far-IR part of the SED; and, if possible, (6) millimeter continuum data that provide a proper characterization of the Rayleigh–Jeans tail, which is crucial for robust dust mass estimates.

To derive a characteristic sSFR_{MS} at a given redshift and a given stellar mass, we define an MS, $\text{SFR}_{\text{MS}}(z, M_*)$, that varies with stellar mass with a slope of 0.81 (e.g., Rodighiero et al. 2011) and evolves with time as $(1+z)^{2.95}$ (e.g., Elbaz et al. 2011; Pannella et al. 2009). In what follows we describe the *Herschel* observations used in this study, as well as the sample of galaxies considered here.

2.1. *Herschel* Data

We use deep 100 and 160 μm PACS and 250, 350, and 500 μm SPIRE observations from the GOODS-*Herschel* program. Details about the observations are given in Elbaz et al. (2011). *Herschel* fluxes are derived from point-spread function (PSF) fitting using *galfit* (Peng et al. 2002). A very extensive set of priors, including all galaxies detected in the ultra-deep Spitzer Multiband Imaging Photometer (MIPS) 24 μm imaging, is used for source extraction and photometry at 100, 160, and 250 μm , which effectively allow us to obtain robust flux estimates for relatively isolated sources, even beyond formal confusion limits at 250 μm . For 350 and 500 μm , this approach does not allow accurate measurements due to the increasingly large PSFs. Hence, we use a reduced set of priors based primarily on Very Large Array (VLA) radio detections, resulting in flux uncertainties consistent with the confusion noise at the IR wavelengths. Our measurements are in good agreement with the alternative catalogs used in Elbaz et al. (2011). The advantage of using *galfit* for PSF fitting is in its detailed treatment of the covariance matrix to estimate error bars in the flux measurements, which is crucial to eventually derive a reliable estimate of flux errors for the case of blended/neighborly sources. The effective flux errors in each band can vary substantially with position, depending on the local density of prior sources over areas comparable to the PSF. A detailed description of the flux measurements and Monte Carlo (MC) derivations of the uncertainties will be presented elsewhere (E. Daddi et al. 2012, in preparation). We correct the PACS photometry for a small flux bias introduced (due to source filtering for background subtraction) during data

reduction (see H-GOODS public data release¹⁴; P. Popesso et al. 2012, in preparation).

2.2. A Sample of Main-sequence Galaxies at $z \sim 1.5$ and $z \sim 0.5$

Daddi et al. (2010a) presented Plateau de Bure Interferometer (PdBI) CO[2–1] emission line detections of six star-forming galaxies at $z \sim 1.5$, originally selected by using the “star-forming BzK” color criterion (Daddi et al. 2004b). All six sources (BzK-21000, BzK-17999, BzK-4171, BzK-16000, BzK-12591, and BzK-22536) have spectroscopic redshifts (now confirmed by multiple CO detections; for optical redshifts see D. Stern et al. 2012, in preparation; Cowie et al. 2004) and robust PACS and/or SPIRE detections. Four of these sources also benefit from 1.3 millimeter continuum data derived as a by-product from the CO[5–4] emission line observations (H. Dannerbauer et al. 2012, in preparation). For BzK-21000, continuum detections and upper limits are also obtained at 1.1, 2.2, and 3.3 mm (Daddi et al. 2010a; Dannerbauer et al. 2009). In addition to IRAC and MIPS 24 μm data, the sources are seen in the 16 μm InfraRed Spectrograph peak-up image (Teplitz et al. 2011). Although we will revisit (and confirm) the SFRs of these sources based on the *Herschel* data, the existing UV, mid-IR, and radio SFR estimates, along with stellar mass measurements derived by fitting the Bruzual & Charlot (2003) model SEDs to their rest-frame UV to near-IR photometry (Daddi et al. 2010a), consistently place them in the $\text{SFR}-M_*$ MS at $z \sim 1.5$ (Daddi et al. 2010a). Finally, the UV rest-frame morphologies, the double-peaked CO profiles, the large spatial extent of their CO reservoirs, and the low gas excitation of the sources all provide strong evidence that they are large, clumpy, rotating disks (Daddi et al. 2010a).

We also consider three $z \sim 0.5$ normal disks with Sérsic index $n < 1.5$ and spectroscopic redshifts, for which we have CO[2–1] emission line detections (Daddi et al. 2010b). Similar to the $z \sim 1.5$ sample, the sources are detected in the PACS and/or SPIRE bands and are part of the $\text{SFR}-M_*$ MS based on their 24 μm derived IR luminosities and SFRs, which are known to be robust in this redshift range (Elbaz et al. 2010, 2011). The *Herschel* and millimeter photometries of the MS galaxies considered here are summarized in Table 1.

2.3. A Sample of High- z SMGs

As a comparison sample to our MS galaxies, we also include in our analysis a small sample of SMGs: GN 20, SMM J2135-0102, and HERMES J105751.1+573027. The selection of the targets was driven by the need for available multi-wavelength photometry, including *Herschel* and millimeter continuum observations, as well as CO[1–0] emission line detections.

GN 20 was already studied in Magdis et al. (2011). It is one of the best-studied SMGs to date, the most luminous, and also one of the most distant ($z = 4.05$; Pope et al. 2006; Daddi et al. 2009) in the GOODS-N field. *Herschel* photometry and the far-IR/millimeter properties of the source have already been presented in detail in Magdis et al. (2011). In brief, the source is detected in all *Herschel* bands (apart from 100 μm) and in the AzTEC 1.1 mm map (Perera et al. 2008), while continuum emission is also measured at 2.2, 3.3, and 6.6 mm (Carilli et al. 2011), as well as at 1.4 GHz with the VLA (Morrison et al. 2010). Furthermore, Carilli et al. (2010) reported the detection

¹⁴ <http://hedam.oamp.fr/GOODS-Herschel/index.php>

Table 1
PACS, SPIRE and 1.3 mm Photometry for MS Galaxies in This Study

Source	R.A. ^a (J2000)	Decl. (J2000)	S ₁₀₀ (mJy)	S ₁₆₀ (mJy)	S ₂₅₀ (mJy)	S ₃₅₀ (mJy)	S ₅₀₀ (mJy)	S _{1.3 mm} (mJy)
ID-8049	188.9751587	62.1787071	10.7 ± 0.7	20.1 ± 1.5	23.0 ± 1.5	23.7 ± 5.2	12.5 ± 4.5	...
ID-5819	189.1774139	62.1594429	12.2 ± 0.7	19.5 ± 1.3	13.6 ± 1.8	5.7 ± 6.5	3.2 ± 7.1	...
ID-7691	188.9502106	62.1763153	14.3 ± 0.7	19.0 ± 1.3	13.6 ± 1.5	7.6 ± 6.5	4.6 ± 7.2	...
BzK-4171	189.1106110	62.1431656	3.4 ± 0.4	10.3 ± 1.1	15.1 ± 3.1	7.5 ± 5.6	7.0 ± 5.8	0.04 ± 0.14
BzK-12591	189.4224091	62.2142181	10.2 ± 0.7	19.3 ± 1.4	25.6 ± 2.0	19.7 ± 4.4	9.2 ± 5.6	...
BzK-25536	189.3679962	62.3152504	0.8 ± 0.7	3.0 ± 0.9	5.2 ± 1.2	0.2 ± 6.1	5.6 ± 5.6	...
BzK-21000	189.2942505	62.3762665	9.1 ± 0.5	17.0 ± 1.4	25.3 ± 4.4	20.1 ± 4.7	11.6 ± 7.5	0.83 ± 0.36
BzK-17999	189.4658661	62.2556038	4.9 ± 0.5	12.5 ± 1.1	15.3 ± 1.3	11.1 ± 5.4	5.9 ± 4.8	0.30 ± 0.10
BzK-16000	189.1253967	62.2410736	1.8 ± 0.5	4.4 ± 0.7	10.2 ± 4.4	9.5 ± 5.2	3.3 ± 5.9	0.53 ± 0.13

Notes. ^a Coordinates are from VLA 1.4 GHz continuum emission (Morrison et al. 2010). The VLA 1.4 GHz map has a resolution of 1''8, and the typical position accuracy for our sources is 0''20.

of the CO[1–0] and CO[2–1] lines with the VLA and CO[6–5] and CO[5–4] lines with the PdBI and the Combined Array for Research in Millimeter Astronomy (CARMA), respectively. A compilation of the photometric data is given in Table 1 of Magdis et al. (2011).

SMM J2135-0102 (SMM-J2135 hereafter) is a highly magnified SMG at $z = 2.325$, with an amplification factor of $\mu = 32.4 \pm 4.5$, serendipitously discovered by Swinbank et al. (2010) behind the cluster MACS J2135-01. The source has exquisite photometric coverage from rest-frame UV to radio including SPIRE broadband data (Swinbank et al. 2010, Table 1; Ivison et al. 2010, Table 1). Swinbank et al. (2010) also report the detection of CO[1–0] and CO[3–2] emission lines using the Zpectrometer on the Green Bank Telescope and PdBI observations, while Ivison et al. (2010), using the SPIRE Fourier Transform Spectrometer (FTS), presented the detection of the [C II]158 μm cooling line.

Finally, HERMES J105751.1+573027 (HSLW-01 hereafter) is a *Herschel*/SPIRE-selected galaxy at $z = 2.957$, multiply lensed (magnification factor $\mu = 10.9 \pm 0.7$) by a foreground group of galaxies. The source was discovered in Science Demonstration Phase *Herschel*/SPIRE observations of the Lockman-SWIRE field as part of the *Herschel* Multi-tiered Extragalactic Survey (HerMES; S. Oliver et al. 2012). The optical to millimeter photometry of the source is presented in Table 1 of Conley et al. (2011), while Riechers et al. (2011a) report the detection of CO[5–4], CO[3–2], and CO[1–0] emission using the PdBI and CARMA and the Green Bank Telescope.

We note that due to the high magnification factor for SMM-J2135 and HSLW-01, these sources might not be representative of the bulk population of SMGs, traditionally selected as $S_{850} > 5$ mJy. Also, a large number of non-lensed SMGs with CO[3–2] observations are available in the literature. However, we choose not to consider them in this study, as the uncertain gas excitation results in dubious CO[1–0] estimates (e.g., Ivison et al. 2010; Riechers et al. 2011b), which are essential for investigating the gas properties of the sources.

2.4. A Statistical Sample of $z \sim 1$ and $z \sim 2$ MS Galaxies

In addition to our samples of individually detected MS galaxies at $z \sim 1.5$ and $z \sim 0.5$, we also perform a stacking analysis to derive the average SED of MS galaxies at $z \sim 1$ and $z \sim 2$. Specifically, we use the $z \sim 1$ GOODS samples of Salmi et al. (2012; see also Daddi et al. 2007; M. Pannella et al. 2012, in preparation). In order to remove bulge-dominated galaxies with low sSFR, we discard objects with a Sérsic index $n > 1.5$

(Salmi et al. 2012), as measured from the GOODS ACS images (Gialavalisco et al. 2004), and consider only 24 μm detected galaxies from the GOODS ultra-deep *Spitzer* imaging. To remove SBs, we proceed as follows: (1) from M_* and redshift, we compute sSFR_{MS}, i.e., the fiducial mean sSFR expected for MS galaxies with a given mass and redshift, derived as described at the start of Section 2; (2) from *Herschel* data we derive L_{IR} and subsequently SFR estimates and exclude galaxies with measured sSFR/sSFR_{MS} > 3. Since not all SB systems are expected to be detected by *Herschel*, we also omit sources with sSFRs/sSFR_{MS} > 3 using the UV-based, corrected-for-extinction, SFR estimates by Daddi et al. (2007) and the *Spitzer* estimates of Salmi et al. (2012). The $z \sim 2$ sources are drawn from the BzK-selected sample of Daddi et al. (2007; now extended to deeper *K*-band depths by M. Pannella et al. 2012, in preparation). Since this color-selection technique naturally excludes quiescent galaxies, we only exclude SBs identified using the same method as for the $z \sim 1$ sample. The total number of $z \sim 1$ and $z \sim 2$ galaxies considered in the stacking analysis is 1569 and 3618, respectively. The average SEDs of these two samples are then measured by stacking, using various standard techniques depending on the wavelength:

1. *16 μm .* We use the Teplitz et al. (2011) maps. The stacking is performed using the IAS stacking library (Béthermin et al. 2010) and PSF-fitting photometry.
2. *24 and 70 μm .* We use the 24 μm and 70 μm (Frayser et al. 2006) maps of GOODS, the IAS stacking library, and aperture photometry with parameters similar to that in Béthermin et al. (2010).
3. *100 and 160 μm .* We use the GOODS-*Herschel* PACS data (Elbaz et al. 2011), the IAS stacking library, and PSF fitting. We apply the appropriate flux correction for faint, non-masked sources to the PACS stacks (P. Popesso et al. 2012, in preparation).
4. *250, 350, and 500 μm .* We use the GOODS-*Herschel* SPIRE (Elbaz et al. 2011) data and the mean of pixels centered on sources as in Béthermin et al. (2012b). The bias due to clustering is estimated to be about 20% at 500 μm and thus negligible compared with the statistical uncertainties. This bias is smaller at shorter wavelengths where the beam is narrower (Béthermin et al. 2012b).
5. *870 μm and 1100 μm .* We used the Weiß et al. (2009) LABOCA map of eCDFs and the Perera et al. (2008) AzTEC map of GOODS-N. Contrary to SPIRE, (sub)millimeter data are noise limited; it is thus optimal to beam-smooth the map before stacking (J. D. Vieira et al.

2012, in preparation). We thus apply the Marsden et al. (2009) method to perform our stacking, which takes the mean of pixels centered on sources in the beam-smoothed map.

At all wavelengths, we used a bootstrap technique to estimate the uncertainties (Jauzac et al. 2011), and the mean fluxes measured in the two fields are combined quadratically to produce a mean SED at $z \sim 1$ and $z \sim 2$. For the $z \sim 2$ normal galaxies, we also construct average SEDs in three stellar mass bins in the range of $9.7 < \log(M_*/M_\odot) < 11.2$ with a bin size of $\Delta \log(M_*/M_\odot) = 0.5$, as well as in four bins of $\text{sSFR}/\text{sSFR}_{\text{MS}}$ over the range $-0.4 < \log(\text{sSFR}/\text{sSFR}_{\text{MS}}) < 0.4$, with a bin size of $\Delta \log(\text{sSFR}/\text{sSFR}_{\text{MS}}) = 0.2$.

3. DERIVATION OF FAR-IR PROPERTIES

Several key physical properties of distant galaxies, such as infrared luminosities (L_{IR}), dust temperatures (T_d), and dust masses (M_{dust}), can be estimated by fitting their mid- to far-IR SEDs with various models and templates calibrated in the local universe. However, the lack of sufficient data for a proper characterization of the SED of distant galaxies has often limited this kind of analysis to models suffering from (necessarily) oversimplified assumptions and large generalizations. The *Spitzer*, *Herschel*, and millimeter data available for the galaxies in our high- z sample provide thorough photometric sampling of their SEDs, allowing the use of more realistic models that previously have been applied mainly in the analysis of nearby galaxies. Here, we consider both the physically motivated Draine & Li (2007, hereafter DL07) models and the more simplistic, but widely used, modified blackbody (MBB) model.

3.1. The Draine & Li (2007) Model

We employ the dust models of DL07, which constitute an update of those developed by Weingartner & Draine (2001) and Li & Draine (2001), and which were successfully applied to the integrated photometry of the Spitzer Nearby Galaxy Survey (SINGS) galaxies (Draine et al. 2007). These models describe the interstellar dust as a mixture of carbonaceous and amorphous silicate grains, whose size distributions are chosen to mimic the observed extinction law in the MW, the Large Magellanic Cloud (LMC), and the Small Magellanic Cloud (SMC) bar region. The properties of these grains are parameterized by the polycyclic aromatic hydrocarbon (PAH) index, q_{PAH} , defined as the fraction of the dust mass in the form of PAH grains. The majority of the dust is supposed to be located in the diffuse interstellar medium (ISM), heated by a radiation field with a constant intensity U_{min} . A smaller fraction γ of the dust is exposed to starlight with intensities ranging from U_{min} to U_{max} , representing the dust enclosed in photodissociation regions (PDRs). Although this PDR component contains only a small fraction of the total dust mass, in some galaxies it contributes a substantial fraction of the total power radiated by the dust. Then, according to DL07, the amount of dust dM_{dust} exposed to radiation intensities between U and $U + dU$ can be expressed as a combination of a δ -function and a power law:

$$\frac{dM_{\text{dust}}}{dU} = (1 - \gamma)M_{\text{dust}}\delta(U - U_{\text{min}}) + \gamma M_{\text{dust}} \frac{\alpha - 1}{U_{\text{min}}^{1-\alpha} - U_{\text{max}}^{1-\alpha}} U^{-\alpha}, \quad (1)$$

with ($U_{\text{min}} \leq U_{\text{max}}$, $\alpha \neq 1$), M_{dust} the total dust mass, γ the fraction of the dust mass that is associated with the power-law

part of the starlight intensity distribution, and U_{min} , U_{max} , and α characterizing the distribution of starlight intensities in the high-intensity regions.

Following DL07, the spectrum of a galaxy can be described by a linear combination of one stellar component approximated by a blackbody with color temperature $T_* = 5000$ K and two dust components, one arising from dust in the diffuse ISM, heated by a minimum radiation field U_{min} (“diffuse ISM” component), and the other from dust heated by a power-law distribution of starlight, associated with the intense PDRs (“PDR” component). Then, the model emission spectrum of a galaxy at distance D is

$$f_\nu^{\text{model}} = \Omega_* B_\nu(T_*) + \frac{M_{\text{dust}}}{4\pi D^2} [(1 - \gamma)p_\nu^{(0)}(q_{\text{PAH}}, U_{\text{min}}) + \gamma p_\nu(q_{\text{PAH}}, U_{\text{min}}, U_{\text{max}}, \alpha)], \quad (2)$$

where Ω_* is the solid angle subtended by stellar photospheres, $p_\nu^{(0)}(q_{\text{PAH}}, U_{\text{min}})$ and $p_\nu(q_{\text{PAH}}, U_{\text{min}}, U_{\text{max}}, \alpha)$ are the emitted power per unit frequency per unit dust mass for dust heated by a single starlight intensity U_{min} , and dust heated by a power-law distribution of starlight intensities $dM/dU \propto U^{-\alpha}$ extending from U_{min} to U_{max} .

In principle, the dust models in their most general form are dictated by seven free parameters (Ω_* , q_{PAH} , U_{min} , U_{max} , α , γ , and M_d). However, Draine et al. (2007) showed that the overall fit is insensitive to the adopted dust model (MW, LMC, and SMC) and the precise values of α and U_{max} . In fact, they showed that fixed values of $\alpha = 2$ and $U_{\text{max}} = 10^6$ successfully described the SEDs of galaxies with a wide range of properties. They also favor the choice of MW dust models for which a set of models with q_{PAH} ranging from 0.4% to 4.6% is available. Furthermore, since small U_{min} values correspond to dust temperatures below ~ 15 K that cannot be constrained by far-IR photometry alone, in the absence of rest-frame submillimeter data, they suggest using $0.7 \leq U_{\text{min}} \leq 25$. While this lower cutoff for U_{min} prevents the fit from converging to erroneously large amounts of cold dust heated by weak starlight ($U_{\text{min}} < 0.7$), the price to pay is a possible underestimate of the total dust mass if large amounts of cold dust are indeed present. However, Draine et al. (2007) concluded that omitting submillimeter data from the fit increases the scatter of the derived masses up to 50% but does not introduce a systematic bias in the derived total dust masses.

Under these assumptions, we fit the mid-IR to millimeter data points of each galaxy in our sample, searching for the best-fit model by χ^2 minimization and parameterizing the goodness of fit by the value of the reduced χ^2 , $\chi_\nu^2 \equiv \chi^2/\text{df}$ (where df is the number of degrees of freedom). The best-fit model yields a total dust mass (M_{dust}), U_{min} , γ , and q_{PAH} , while to derive L_{IR} ¹⁵ estimates, we integrate the emerging SEDs from 8 to 1000 μm :

$$L_{\text{IR}} = \int_{8\mu\text{m}}^{1000\mu\text{m}} L_\nu(\lambda) \times \frac{c}{\lambda^2} d\lambda. \quad (3)$$

A by-product of the best-fit model is also the dust-weighted mean starlight intensity scale factor, $\langle U \rangle$, defined as

$$\langle U \rangle = \begin{cases} \frac{L_{\text{dust}}}{P_0 M_{\text{dust}}} & \text{or} \\ \left[(1 - \gamma)U_{\text{min}} + \frac{\gamma \ln(U_{\text{max}}/U_{\text{min}})}{U_{\text{min}}^{-1} - U_{\text{max}}^{-1}} \right], & \text{for } \alpha = 2, \end{cases} \quad (4)$$

¹⁵ L_{dust} quoted below is similar to L_{IR} , but integrated from 0 to ∞ .

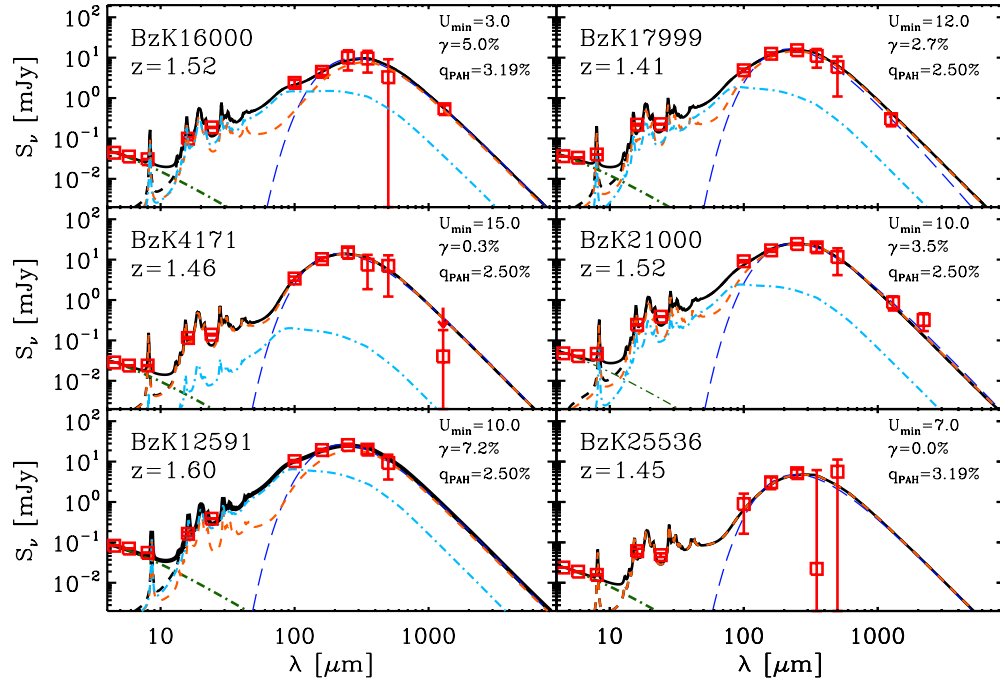


Figure 1. Observed SEDs of $z \sim 1.5$ BzK galaxies, overlaid with the best-fit Draine & Li (2007) models (black) and the best-fit single-temperature modified blackbody (blue). The black dashed line is the DL07 model without the stellar component that is depicted with a green dot-dashed line. Orange dashed and cyan dot-dashed lines show separate contributions of starlight and emission from dust heated by $U = U_{\min}$ (diffuse ISM component) and dust heated by $U_{\min} < U < U_{\max}$ (“PDR” component), respectively. The fitted parameters from the best-fit Draine & Li (2007) model fits are listed within each panel.

(A color version of this figure is available in the online journal.)

Table 2
Physical Properties of Individually Detected Sources, Based on Draine & Li (2007) Models

Source	z_{spec}	χ^2_{ν}	$\log L_{\text{IR}}$ (L_{\odot})	$\log M_{\text{d}}$ (DL07) (M_{\odot})	U_{\min}	γ (%)	q_{PAH} (%)	$\langle U \rangle$	T_{d}^{a} (K)	β^{a}
ID-8049	0.507	2.1	11.22 ± 0.02	8.81 ± 0.13	2.0	0.4	2.50	2.0	22 ± 2	1.5^{b}
ID-5819	0.530	1.78	11.26 ± 0.01	8.22 ± 0.10	7.0	2.4	2.50	8.8	31 ± 1	1.5^{b}
ID-7691	0.637	0.65	11.54 ± 0.03	8.28 ± 0.10	8.0	7.6	2.50	14.5	31 ± 2	1.5^{b}
BzK-4171	1.465	1.56	11.98 ± 0.04	8.70 ± 0.09	15.0	0.3	2.50	15.4	37 ± 2	1.5^{b}
BzK-12591	1.600	1.04	12.44 ± 0.02	9.09 ± 0.09	10.0	7.2	2.50	17.6	37 ± 1	1.5^{b}
BzK-25536	1.459	1.94	11.46 ± 0.06	8.52 ± 0.26	7.0	0.0	3.19	7.0	33 ± 3	1.5^{b}
BzK-21000	1.523	1.12	12.32 ± 0.01	9.07 ± 0.06	10.0	3.5	2.50	13.7	35 ± 2	1.4 ± 0.2
BzK-16000	1.522	1.71	11.87 ± 0.03	9.11 ± 0.07	3.0	5.0	3.19	4.7	30 ± 1	1.5 ± 0.2
BzK-17999	1.414	0.86	12.06 ± 0.02	8.78 ± 0.07	12.0	2.7	2.50	15.3	33 ± 1	1.9 ± 0.2
GN 20	4.055	1.44	13.25 ± 0.06	9.67 ± 0.06	25.0	1.8	1.20	29.6	33 ± 2	2.1 ± 0.2
SMM-J2135 ^c	2.325	3.41	12.30 ± 0.06	8.85 ± 0.06	20.0	1.5	0.47	21.9	30 ± 1	2.0 ± 0.2
HSLW-01 ^c	2.957	6.61	13.13 ± 0.06	8.93 ± 0.08	25.0	30.0	0.47	134.0	39 ± 2	2.1 ± 0.2
Stack-z1 ^d	0.98	3.91	11.21 ± 0.09	8.14 ± 0.13	8.0	2.0	3.90	9.7	32 ± 2	1.5^{b}
Stack-z2 ^d	1.97	2.01	11.55 ± 0.06	8.27 ± 0.11	12.0	2.5	3.19	15.1	38 ± 2	1.5^{b}

Notes.

^a Derived based on single-temperature MBB.

^b β fixed to this value in the MBB fit.

^c Values corrected for magnification.

^d Best-fit values accounting for the redshift distribution of the sample.

where P_0 is the power absorbed per unit dust mass in a radiation field with $U = 1$. Note that essentially $\langle U \rangle$ is proportional to $L_{\text{IR}}/M_{\text{dust}}$, and as we will discuss later for the definition of L_{IR} adopted here, i.e., $L_{8-1000 \mu\text{m}}$, our data suggest that $P_0 \approx 125$. Uncertainties in L_{IR} and M_{dust} are quantified using MC simulations. To summarize, for each galaxy a Gaussian random number generator was used to create 1000 artificial flux sets from the original fluxes and measurement errors. These new data sets were then fitted in the same way, and the standard deviation in the new parameters was taken to represent the uncertainty in

the parameters found from the real data set. Best-fit values along with their corresponding uncertainties are listed in Table 2 for all sources in our sample. To check for possible contamination of the submillimeter continuum broadband photometry from C+ (158 μm) emission (e.g., Smail et al. 2011), we repeated the fit excluding the affected bands (i.e., 350 μm and 500 μm for $z \sim 0.5$ and $z \sim 1.5$ –2.0, respectively), without noticing any effect in the derived parameters. The best-fit models along with the observed SEDs of the $z \sim 1.5$ and $z \sim 0.5$ galaxies and SMGs are shown in Figures 1–3, respectively.

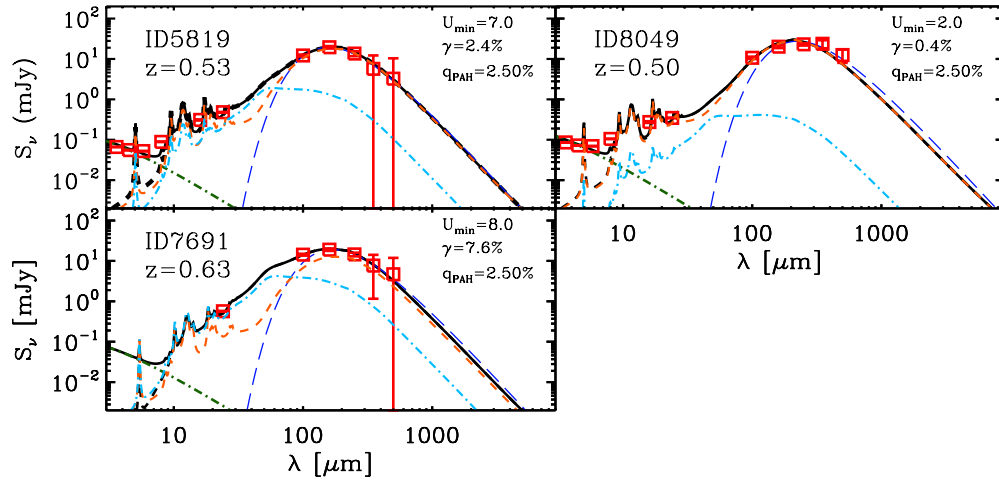


Figure 2. Same as Figure 1, but for the $z \sim 0.5$ galaxies in our sample.
(A color version of this figure is available in the online journal.)

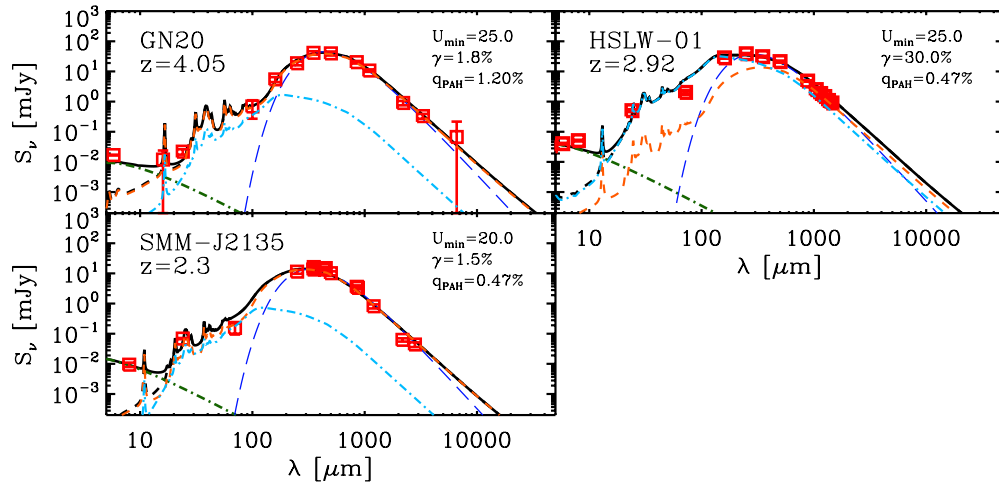


Figure 3. Same as Figure 1, but for the SMGs considered in this study.
(A color version of this figure is available in the online journal.)

3.2. The Importance of Millimeter Data

While *Herschel* data accurately probe the peak of the SED in the far-IR emission of distant galaxies, rest-frame submillimeter observations ($\lambda_{\text{rest}} \geq 250 \mu\text{m}$) are necessary to sample the Rayleigh–Jeans tail. Since the available far-IR photometry for five of our sources is restricted to *Herschel* observations, it is important to explore possible biases or systematics introduced by the lack of millimeter continuum data. Given the ever-increasing number of distant galaxies with *Herschel* photometry, this investigation will also provide guidance for similar studies in the future. To assess the significance of adding millimeter photometry in the derivation of the far-IR properties of the galaxies, and particularly their dust mass, we repeat the fitting procedure, this time excluding any data at wavelengths longer than rest-frame $200 \mu\text{m}$, for the four $z \sim 1.5$ BzK and the three SMGs with available millimeter continuum observations.

A comparison between the derived dust masses with and without the use of millimeter data is shown in Figure 4 (left). We find no evidence for a strong systematic bias, with an average ratio between the two estimates ($\langle M_{\text{dust}}^{\text{mm}} / M_{\text{dust}}^{\text{nomm}} \rangle = 0.80 \pm 0.2$). Interestingly, the sources with the largest discrepancies are the

SMGs, although the sample is too small to clearly demonstrate the existence of a systematic effect. However, the addition of millimeter data has a noticeable impact on the uncertainties of the derived M_{dust} estimates, which are reduced, on average, by a factor of ~ 2 . Studies in the local universe reach similar conclusions, with the addition that in the absence of rest-frame submillimeter data, dust masses tend to be underestimated for metal-poor galaxies. This could serve as an indirect indication that our sample mainly consists of metal-rich sources, something that we will also argue in Section 4.

The derived γ and U_{min} are also in broad agreement between the two cases. However, we notice a weak systematic bias toward higher $\langle U \rangle$ values, i.e., stronger mean radiation fields, when millimeter data are considered in the fit, reflecting the fact that $\langle U \rangle \propto L_{\text{IR}} / M_{\text{dust}}$. We conclude that such trends in $\langle U \rangle$ and M_{dust} suggest that millimeter data can place better constraints on the diffuse ISM emission, as well as on the relative contribution of a PDR component to the total radiation field, and consequently on the M_{dust} of individual high- z galaxies. Finally, we note that the detailed sampling of the peak of the far-IR emission provided by *Herschel* data can result in robust L_{IR} estimates without the need of millimeter data.

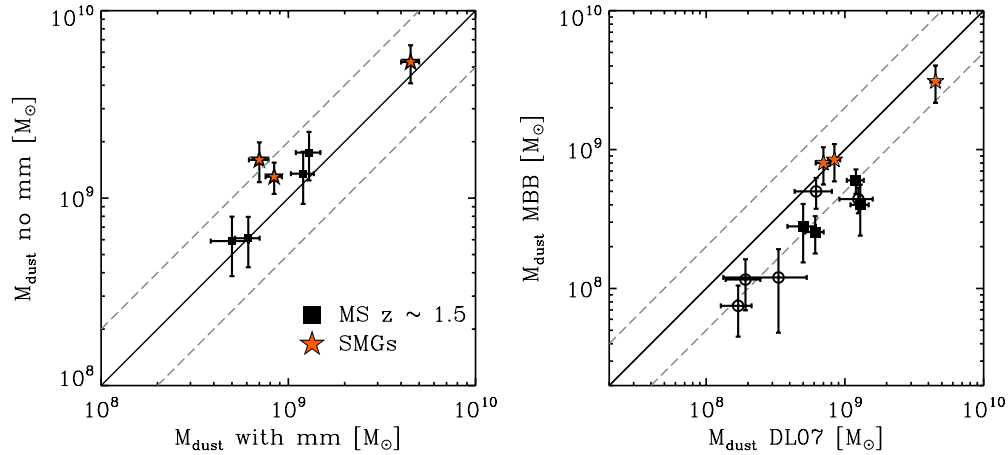


Figure 4. Left: comparison between the DL07 M_{dust} estimates inferred with and without the addition of millimeter data to the fit, demonstrating the significance of the addition of millimeter continuum data for the derivation of dust masses. Although the two estimates seem to be overall in good agreement, we note that in absence of millimeter continuum data we tend to overestimate the M_{dust} in SMGs. Right: comparison between dust masses derived based on a single-temperature modified blackbody (MBB) and those derived by the Draine & Li (2007) models. Filled squares and open circles indicate sources with and without millimeter data, respectively. For the former β was treated as a free parameter in the MBB fit, while for the latter it was fixed to $\beta = 1.5$. Orange stars represent the SMGs considered in this study. In both panels, the black solid line corresponds to unity and the two gray dashed lines its offset by a factor of 2 and 0.5.

(A color version of this figure is available in the online journal.)

3.3. Comparison with Modified Blackbody Fits

Another method for deriving estimates for the dust masses and other far-IR properties, such as dust temperatures and dust emissivity indices (β), is to fit the far-IR to submillimeter SED of the galaxies with a single-temperature MBB, expressed as

$$f_\nu \propto \frac{\nu^{3+\beta}}{e^{\frac{h\nu}{kT_d}} - 1}, \quad (5)$$

where T_d is the effective dust temperature and β is the effective dust emissivity index. Then, from the best-fit model, one can estimate M_{dust} from the relation

$$M_d = \frac{S_\nu D_L^2}{(1+z) \kappa_{\text{rest}} B_\nu(\lambda_{\text{rest}}, T_d)}, \quad \text{with } \kappa_{\text{rest}} = \kappa_0 \left(\frac{\lambda_o}{\lambda_{\text{rest}}} \right)^\beta, \quad (6)$$

where S_ν is the observed flux density, D_L is the luminosity distance, and κ_{rest} is the rest-frame dust mass absorption coefficient at the observed wavelength. While this is a rather simplistic approach, mainly adopted due to the lack of sufficient sampling of the SED of distant galaxies, it has been one of the most widely used methods in the literature. Therefore, an analysis based on MBB models provides not only estimates of the effective dust temperature and dust emissivity of the galaxies in our sample but also a valuable comparison between dust masses inferred with the MBB and DL07 methods.

We fit the standard form of an MBB, considering observed data points with $\lambda_{\text{rest}} > 60 \mu\text{m}$, to avoid emission from very small grains that dominate at shorter wavelengths. For the cases where millimeter data are available we let β vary as a free parameter, while for the rest we have assumed a fixed value of $\beta = 1.5$, typical of disk-like, MS galaxies (Magdis et al. 2011; Elbaz et al. 2011). From the best-fit model, we then estimate the total M_{dust} through Equation (6). For consistency with the DL07 models, we adopt a value of $\kappa_{250 \mu\text{m}} = 5.1 \text{ cm}^2 \text{ g}^{-1}$ (Li & Draine 2001). To obtain the best-fit models and the corresponding uncertainties of the parameters, we followed the

same procedure as for the DL07 models. The derived parameters are summarized in Table 2, and the best-fit models are shown in Figures 1–3.

A comparison between dust masses derived by DL07 and MBB models is shown in Figure 4 (right). We see that an MBB appears to infer dust masses that are lower than those derived based on DL07 models on average by a factor of ~ 2 ($\langle M_{\text{dust}}^{\text{DL07}} / M_{\text{dust}}^{\text{MBB}} \rangle = 1.96 \pm 0.5$). A similar trend was recently reported by Dale et al. (2012), who found that the discrepancy between the two dust mass estimates is smaller for sources with warmer S_{70}/S_{160} colors. Interestingly, when we convolve the best-fit DL07 rest-frame SEDs of our galaxies with the 70 and 160 μm PACS filters, we find that the sources with the warmest S_{70}/S_{160} are indeed those with the best agreement in the dust masses derived from the two methods. The reason behind this discrepancy has been addressed by Dunne et al. (2000). The grains of a given size and material are exposed to different intensities of the interstellar radiation field and thus attain different equilibrium temperatures, which will contribute differently to the SED. The single-temperature models cannot account for this range of T_d in the ISM and attempt to simultaneously fit both the Wien side of the graybody, which is dominated by warm dust, and the Rayleigh–Jean tail, sensitive to colder dust emission. The net effect is that the temperatures are driven toward higher values, consequently resulting in lower dust masses. While restricting the fit to $\lambda \leq 100 \mu\text{m}$ does not provide an adequate solution to the problem (Dale et al. 2012), a two-temperature blackbody fit is more realistic and returns dust masses that are larger by a factor of ~ 2 compared to those derived based on a single T_d MBB (Dunne & Eales 2001), in line with those inferred by the DL07 technique.

Despite the large uncertainties associated with the MBB analysis, it is worth noting that for all SMGs in our sample we measure an effective dust emissivity index $\beta \sim 2.0$, in agreement with the findings of Magnelli et al. (2012). On the other hand, the far-IR to millimeter SEDs of all BzK galaxies are best described by $\beta \sim 1.5$, similar to that found by Elbaz et al. (2011) for MS galaxies. However, we stress that the effective β does not necessarily reflect the intrinsic β of the dust grains due to the degeneracy between β and the temperature distribution

of dust grains in the ISM. The β - T_d degeneracy also prevents a meaningful comparison between the derived T_d for the galaxies in our sample.

4. THE GAS CONTENT OF MAIN-SEQUENCE AND STARBURSTING GALAXIES

Several studies in the local universe have revealed that the total gas-to-dust mass ratio (δ_{GDR}) is correlated with the gas-phase oxygen abundance, in the sense that more metal-rich galaxies tend to exhibit lower δ_{GDR} values (e.g., Muñoz-Mateos et al. 2009; Leroy et al. 2011, and references within). In addition to crucial information regarding the amount of metals trapped in the dust, this correlation can serve as a valuable tool for deriving indirect estimates of the CO to molecular gas mass (M_{H_2}) conversion factor. In particular, if we know the metallicity, the dust mass, and the mass of the atomic gas mass (M_{HI}) of a galaxy, then we can estimate the δ_{GDR} through the $\delta_{\text{GDR}}-Z$ relation and M_{H_2} through the following relation:

$$\delta_{\text{GDR}} M_{\text{dust}} \equiv M_{\text{gas}} = M_{\text{H}_2} + M_{\text{HI}}. \quad (7)$$

Subsequently, if L'_{CO} is measured, then we can estimate α_{CO} , since $M_{\text{H}_2} = \alpha_{\text{CO}} \times L'_{\text{CO}}$. This method has successfully been applied in the local universe (e.g., Leroy et al. 2011) and has recently been extended to high- z galaxies by the pilot study of Magdis et al. (2011). Even though restricted to only two galaxies, which are also part of this study (GN 20 and BzK-21000), Magdis et al. (2011) showed that this approach provides α_{CO} estimates that are consistent with other independent measurements and dynamical arguments. Although it has been a common practice to adopt a value of $\alpha_{\text{CO}} = 0.8$, typical of local ULIRGs, for high- z ULIRGs, our earlier study suggested that such low values apply only to the subset of genuinely starbursting systems at high redshift, while high- z MS galaxies, even those with $L_{\text{IR}} > 10^{12} L_{\odot}$ (i.e., those classified as ULIRGs), have larger α_{CO} values, similar to those of local spirals. Here, we wish to extend this experiment, this time using a substantially larger sample, and to investigate possible correlations between α_{CO} and SB versus MS indicators.

4.1. Estimating Metallicities

A key ingredient of this method is the metallicity of the galaxies, for which we have to rely on indirect measurements. We first derive stellar mass estimates by fitting the Bruzual & Charlot (2003) model SEDs to their rest-frame UV to near-IR spectrum. Then for the $z \sim 1.5$ BzK galaxies and SMM J2135-0102 we use the M_* - Z relation at $z \sim 2$ from Erb et al. (2006), while for the $z \sim 0.5$ sources we adopt the fundamental metallicity relation (FMR) of Mannucci et al. (2010), which relates the SFR and the stellar mass to metallicity. To check for possible systematics, we also derive metallicity estimates for the $z \sim 1.5$ sources with the FMR relation and find that the two methods provide very similar results. For GN 20 and HLSW-1, the situation is more complicated, as the FMR formula is only applicable up to $z \sim 2.5$, and the Erb et al. (2006) relation saturates above $M_* \sim 10^{11} M_{\odot}$. For these two sources, we adopt the line of reasoning of Magdis et al. (2011). Namely, in addition to the metallicity estimates based on the FMR relation, we also consider the extreme case where the huge SFR of the two sources ($\sim 1500 M_{\odot} \text{ yr}^{-1}$) is due to a final burst of star formation triggered by a major merger that will eventually transform the galaxy into a massive elliptical. Once star formation ceases, the mass and metallicity of the resulting

Table 3
Stellar Mass, Metallicity, and Gas Properties

Source	$\log M_*$ (M_{\odot})	Z_{PP04}^a	$\log L_{\text{CO}}$ ($L_{\odot} \text{ K}^{-1} \text{ km}^{-1} \text{ s pc}^{-2}$) ($M_{\odot} \text{ K}^{-1} \text{ km}^{-1} \text{ s pc}^{-2}$)	α_{CO}
ID-8049	10.97	8.80	9.47	13.4 ± 5.5
ID-5819	10.81	8.76	9.53	3.7 ± 1.3
ID-7691	10.83	8.74	9.78	2.4 ± 1.0
BzK-4171	10.60	8.59	10.32	2.5 ± 1.1
BzK-12591	11.04	8.63	10.50	3.8 ± 2.0
BzK-25536	10.51	8.56	10.07	3.1 ± 2.1
BzK-17999	10.59	8.58	10.23	3.9 ± 1.2
BzK-16000	10.63	8.53	10.32	9.7 ± 3.1
BzK-21000	10.89	8.60	10.34	5.7 ± 2.0
GN 20	11.36	9.00	11.21	1.0 ± 0.3
SMM-J2135	10.34	8.50	10.30	3.2 ± 1.0
HLSW-01	10.77	8.80	10.30	1.3 ± 0.4

Notes. ^a Derived using the M_* - Z relation of Erb et al. (2006), Mannucci et al. (2010), or theoretical arguments (GN 20 and HLSW-01). We assume a typical uncertainty of ± 0.2 for all cases.

galaxy will not change further, and one might therefore apply the mass-metallicity relation of present-day elliptical galaxies (e.g., Calura et al. 2009). Combining the metallicity estimates based on this scenario with those derived based on the FMR relation, we estimate that the metallicities could fall in the ranges $12 + \log[\text{O}/\text{H}] = 8.8\text{--}9.2$ for GN 20 and $8.6\text{--}9.0$ for HLSW-1. For the analysis, we will adopt $12 + \log[\text{O}/\text{H}] = 9.0 \pm 0.2$ for GN 20 and $12 + \log[\text{O}/\text{H}] = 8.8 \pm 0.2$ for HLSW-1. We also adopt a typical uncertainty of 0.2 for the rest of the sources. The assumed metallicities, all calibrated at the Pettini & Pagel (2004) (PP04) scale, along with the stellar masses, are given in Table 3.

4.2. Derivation of the CO to M_{H_2} Conversion Factor

To derive α_{CO} estimates for our sample, we first derive a $\delta_{\text{GDR}}-Z$ relation using the local sample presented by Leroy et al. (2011), after converting all metallicities to the PP04 scale (Figure 5, left). The data yield a tight correlation between the two quantities¹⁶ described as $\log \delta_{\text{GDR}} = (10.54 \pm 1.0) - (0.99 \pm 0.12) \times (12 + \log(\text{O}/\text{H}))$, with a scatter of 0.15 dex. Having obtained the M_{dust} and metallicity estimates, we then use the $\delta_{\text{GDR}}-Z$ relation to derive M_{gas} and subsequently estimate α_{CO} from the equation $M_{\text{gas}} = \alpha_{\text{CO}} \times L'_{\text{CO}}$. For the last step, we have assumed that at high- z , $M_{\text{H}_2} \gg M_{\text{HI}}$ or equivalently that $M_{\text{gas}} \approx M_{\text{H}_2}$, as supported by both observational evidence (e.g., Daddi et al. 2010a; Tacconi et al. 2010; Geach et al. 2011) and theoretical arguments (Blitz & Rosolowsky 2006; Bigiel et al. 2008; Obreschkow et al. 2009). All values and their corresponding uncertainties, which take into account both the dispersion of the $\delta_{\text{GDR}}-Z$ relation and the uncertainties in Z and M_{dust} , are summarized in Table 3. In Figure 5 (right), we plot the derived α_{CO} values as a function of metallicity, along with the estimates of Leroy et al. (2011) for a sample of local normal galaxies, as well as for a sample of local ULIRGs from Downes & Solomon (1998), for which we were able to compute their metallicities on the PP04 scale. Fitting high- z MS galaxies along

¹⁶ Adopting the relation quoted by Leroy et al. (2011), i.e., $\log \delta_{\text{GDR}} = (9.4 \pm 1.1) - (0.85 \pm 0.13) \times (12 + \log[\text{O}/\text{H}])$, has virtually no impact on the results presented here, with a mean difference between the derived α_{CO} estimates of a factor of ~ 1.15 .

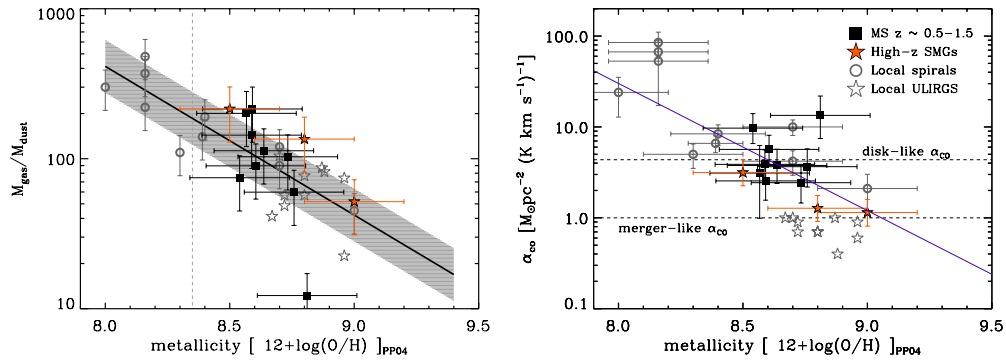


Figure 5. Left: $M_{\text{gas}}/M_{\text{dust}}$ vs. metallicity for a sample of galaxies in the Local Group by Leroy et al. (2011; gray circles) and local ULIRGs by Downes & Solomon (1998; gray stars). The solid black line is the best linear regression fit to Leroy’s sample, and the gray shadowed area depicts the dispersion of the correlation. Filled black squares and orange stars indicate the position of $z \sim 0.5$ – 1.5 MS galaxies and high- z SMGs, respectively, based on the α_{CO} vs. metallicity relation derived in the right panel (Equation (8)). The vertical dashed line indicates the limiting metallicity for which the presented relation is used in this study. Right: inferred α_{CO} values based on the δ_{GDR} method, against metallicity for high- z MS galaxies (black squares) and SMGs (orange stars). Similar to the left panel, we include local disks and ULIRGs by Leroy et al. (2011) and Downes & Solomon (1998). All metallicities have been calculated on the PP04 scale. The blue solid line represents the best regression fit to the data (excluding local ULIRGs), with a slope of -1.39 .

(A color version of this figure is available in the online journal.)

with the local sample of Leroy et al. (2011) yields

$$\log(\alpha_{\text{CO}}) = -(1.39 \pm 0.3) \times (12 + \log(\text{O}/\text{H}))_{\text{PP04}} + 12.8 \pm 2.2, \quad (8)$$

with α_{CO} decreasing for higher metallicities, in agreement with previous studies (e.g., Wilson 1995; Israel 1997; Schrubba et al. 2012, and references within). It is evident that MS galaxies at any redshift have higher α_{CO} values than those of local starbursting ULIRGs and more similar to those of local normal galaxies. In particular, for high- z MS galaxies, we find a mean α_{CO} of 5.5 ± 0.4 , very close to the MW value of 4.6 (e.g., Strong & Mattox 1996; Dame et al. 2001). Interestingly, SMM-J2135 falls close to the locus of MS galaxies with $\alpha_{\text{CO}} \sim 3$, while for the remaining SMGs we find $\alpha_{\text{CO}} \sim 1$, close to the average value of local ULIRGs ($\alpha_{\text{CO}} \sim 0.8$; e.g., Solomon et al. 1997; Tacconi et al. 2008). Finally, simply as a consistency check, we derive and plot in Figure 5 (left) the $M_{\text{gas}}/M_{\text{dust}}$ values of our targets, using α_{CO} estimates as obtained from Equation (8).

4.3. Limitations

Before trying to interpret our findings regarding the α_{CO} values, it is important to discuss possible caveats and limitations of the method. A key ingredient for the derivation of α_{CO} is the M_{dust} estimate. These estimates rely heavily on the adopted model of the grain-size distribution. Dust masses based on different grain-size compositions and opacities in the literature can vary even by a factor of ~ 3 , indicating that the absolute values should be treated with caution (e.g., Galliano et al. 2011). However, the relative values of dust masses derived based on the same assumed dust model should be correct and provide a meaningful comparison, as long as the dust has similar properties in all galaxies. Therefore, any trends arising from the derived M_{dust} estimates are essentially insensitive to the assumed dust model.

One important assumption of our technique is that the $\delta_{\text{GDR}}-Z$ relation defined by local galaxies does not evolve substantially with cosmic time. These quantities are very intimately related, as dust is ultimately made of metals. For example, solar metallicity of $Z_{\odot} = 0.02$ means that 2% of the gas is in metals. The local $\delta_{\text{GDR}}-Z$ relation suggests an average trend where 1% of the gas is in dust. This means that about 50% of the metals are locked

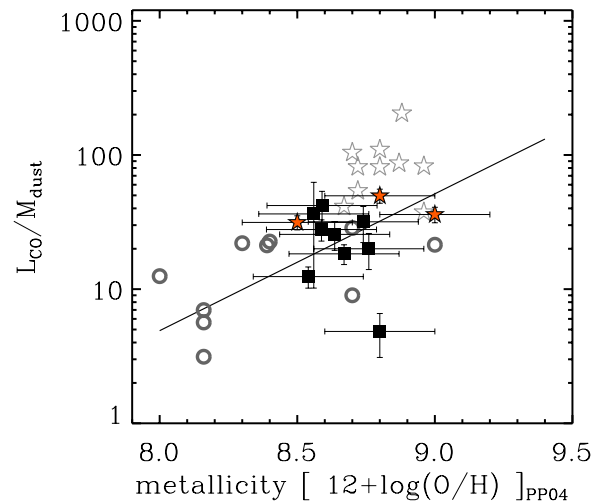


Figure 6. $L'_{\text{CO}}/M_{\text{dust}}$ against metallicity for the same sample of galaxies as in Figure 5. This plot serves as a sanity check for the assumption that the $M_{\text{gas}}/M_{\text{dust}}$ vs. metallicity relation does not evolve considerably with cosmic time.

(A color version of this figure is available in the online journal.)

into dust. This is already quite an efficient process of metal condensations into dust, and it is hard to think how this could be even more efficient at high z (where, e.g., less time is available for the evolution of low-mass stars into the asymptotic giant branch phase), with a much higher proportion of metals locked into the dust phase, a situation that would lead to an overestimate of M_{gas} with our technique. Similarly, chemical evolution studies suggest a small evolution of dust-to-metal ratio, i.e., by a maximum factor of ~ 2 from 2 Gyr after the big bang up to the present time (e.g., Edmunds 2001; Inoue 2003; Calura et al. 2008). Furthermore, if we plot the ratio of the direct observables, $L'_{\text{CO}}/M_{\text{dust}}$, as a function of metallicity, both local and high- z galaxies follow the same trend, suggesting that the local $\delta_{\text{GDR}}-Z$ relation is valid at high z (Figure 6). Finally, while the Leroy et al. (2011) sample yields a slope of -1.0 in the $\delta_{\text{GDR}}-Z$ relation, Muñoz-Mateos et al. (2009) find a rather steeper slope of -2.45 . However, adopting the Muñoz-Mateos relation (after rescaling it to PP04 metallicity) returns very similar α_{CO} values, as the two relations intercept at metallicities very close to the average metallicity of our sample ($12 + \log(\text{O}/\text{H}) \approx 8.6$).

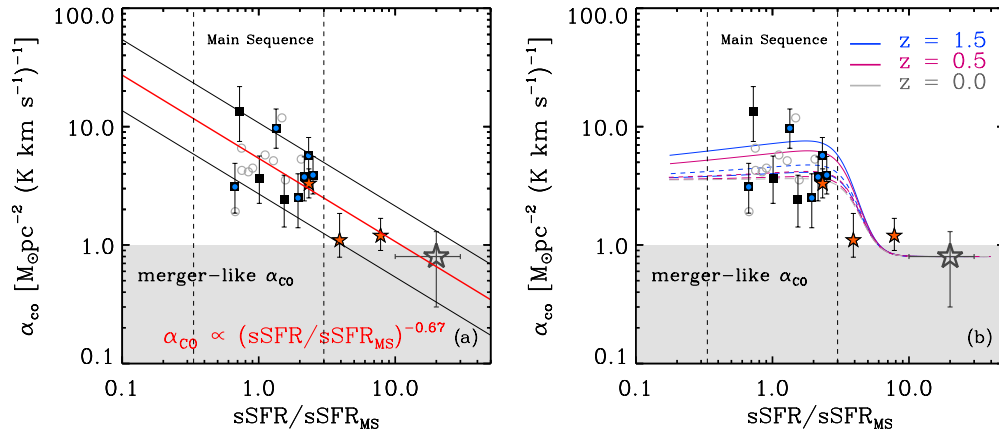


Figure 7. Inferred α_{CO} values against the offset from the main sequence. (a) Inferred α_{CO} values for the MS galaxies (black squares) and SMGs (orange stars) considered in this study against their offset from the main sequence, parameterized as $\text{sSFR}/\text{sSFR}_{\text{MS}}$. Empty gray circles represent local disks from Leroy et al. (2008) and Schruba et al. (2012), while the empty gray star represents the locus of local ULIRGs. The data (only high- z galaxies) are best fit with a slope of -0.67 (red solid line) with a scatter of 0.3 dex and a Spearman’s rank correlation coefficient of $\rho = -0.51$. (b) Same as the left panel but for the case of a metallicity-dependent α_{CO} . Tracks show the variation predicted by M. Sargent et al. (2012, in preparation) based on (1) the relative importance of the starburst and main-sequence mode of star formation as a function of $\text{sSFR}/\text{sSFR}_{\text{MS}}$ and (2) a “metallicity-dependent” α_{CO} , where the metallicity of main-sequence galaxies is inferred based on the stellar mass–star formation–metallicity relation of Mannucci et al. (2010). Blue (purple), solid, dashed, and long-dashed lines correspond to $z = 1.5$ ($z = 0.5$) for $M_* = 1.0 \times 10^{10} M_{\odot}$, $5.0 \times 10^{10} M_{\odot}$, and $1.0 \times 10^{11} M_{\odot}$. The gray long-dashed line corresponds to $z = 0.0$ and $M_* = 1.0 \times 10^{11} M_{\odot}$. (A color version of this figure is available in the online journal.)

We note though that for GN 20 and HLSW (the sources with the highest Z estimates), the Muñoz–Mateos relation would reduce α_{CO} values by a factor of ~ 3 .

4.4. α_{CO} as a Function of Specific Star Formation Rate

With robust L_{IR} measurements in hand, we are in a position to derive accurate estimates of the SFR and sSFR for galaxies in our sample. We first convert the derived L_{IR} to SFRs by using the Kennicutt (1998) relation, scaled for a Chabrier IMF for consistency with our stellar mass estimates. We then infer the sSFR of each source and compare it to the characteristic sSFR_{MS} of the MS galaxies at the corresponding redshift of the source, using the methodology described in Section 2 up to $z = 2.5$. For the two SMGs at $z \sim 3$ and $z \sim 4$, we use the $\text{SFR}-M_*$ relations of Magdis et al. (2010b) and Daddi et al. (2009), respectively. In order to conservatively identify MS galaxies, we classify SBs as galaxies with an excess sSFR relative to that of the MS galaxies by at least a factor of three, i.e., with $\text{sSFR}/\text{sSFR}_{\text{MS}} > 3$. We note, however, that the $\text{sSFR}/\text{sSFR}_{\text{MS}}$ indicator is only a statistical measure of the star formation mode of the galaxies, and there is no rigid limit that separates MS from SB galaxies.

Our analysis suggests that high- z MS galaxies, associated with a secular star formation mode, exhibit higher α_{CO} values at any redshift compared to those of merger-driven local ULIRGs. Since the latter are known to be strong outliers from the local $\text{SFR}-M_*$ relation, we expect a dependence of the α_{CO} value with sSFR. However, the functional dependence between the two quantities is not straightforward. In the local universe, there is evidence for a bimodality in the α_{CO} value, linked with the two known star formation modes: normal disks (for $Z \sim Z_{\odot}$) are associated with $\alpha_{\text{CO}} \sim 4.4$ and merger-driven ULIRGs with $\alpha_{\text{CO}} \sim 0.8$. As we will discuss later, if the α_{CO} of normal galaxies depends only on metallicity, then we expect only a weak increase of α_{CO} as a function of $\text{sSFR}/\text{sSFR}_{\text{MS}}$ within the MS. Consequently, in order to incorporate the observed steep decrease of α_{CO} in SB systems, α_{CO} and the relative offset from the MS (i.e., $\text{sSFR}/\text{sSFR}_{\text{MS}}$) will be related with a step function. On the other hand, if α_{CO} also depends on other parameters than

metallicity, such as the compactness and/or the clumpiness of the ISM of normal galaxies, and if the ISM conditions of MS galaxies do vary significantly, then α_{CO} could smoothly decrease as we depart from the MS and move toward the SB regime (e.g., Narayanan et al. 2012).

The scenario of a continuous variation of α_{CO} with $\text{sSFR}/\text{sSFR}_{\text{MS}}$ is depicted in Figure 7(a). In addition to our galaxies, we also include a sample of local normal galaxies for which we have robust M_* and SFR estimates from Leroy et al. (2008) and α_{CO} measurements from Schruba et al. (2012). A linear regression fit yields the following relation:

$$\alpha_{\text{CO}} = (5.8 \pm 2.0) \times [\text{sSFR}/\text{sSFR}_{\text{MS}}]^{(-0.67 \pm 0.25)}, \quad (9)$$

with a scatter of 0.3 dex. We stress that, given the lack of a sufficient number of SBs in our sample, this relation is poorly constrained in the SB regime. Nevertheless, the locus of local ULIRGs seems to be consistent with the emerging trend. Note that since we lack a sample of local ULIRGs for which both α_{CO} and sSFR are accurately determined, the position of local ULIRGs in Figure 7 indicates the average α_{CO} and sSFR of the population, as derived by Downes & Solomon (1998) and da Cunha et al. (2010b), respectively. To further check the robustness of the fit, we also perturbed the original data within the errors and repeated the fit for 1000 realizations. The mean slope derived with this method is very close to the one describing the original data. A Spearman’s rank correlation test yields a correlation coefficient of $\rho = -0.51$, with a p -value of 0.03, suggesting a moderately significant correlation between $\text{sSFR}/\text{sSFR}_{\text{MS}}$ and α_{CO} . However, repeating the Spearman’s test, this time excluding starbursting systems, does not yield a statistically significant correlation, with $\rho = -0.15$ and a p -value of 0.3, indicating a very small dependence, if any, between α_{CO} and sSFR within the MS.

It is therefore unclear whether α_{CO} varies *inside* the MS or if instead there is a bifurcation between the mean values appropriate for MS versus SB galaxies. If the α_{CO} conversion factor primarily depends on metallicity, one would expect little or no variations with sSFR at constant mass within the MS.

Detailed computations for this scenario are presented in M. Sargent et al. (2012, in preparation), in which burst-like activity is assumed to be characterized by a constant, low conversion factor, chosen here to be $\alpha_{\text{CO}}^{\text{SB}} = 0.8$. To predict the variations of α_{CO} as a function of $\text{sSFR}/\text{sSFR}_{\text{MS}}$ according to this scenario, Sargent et al. (2012) compute the relative importance of MS and SB activities at a given position within the stellar mass versus SFR plane using the decomposition of the sSFR distribution at fixed stellar mass derived in Sargent et al. (2012; based on the data of Rodighiero et al. 2011). Metallicities, which form the basis for computing α_{CO} for an ISM experiencing “normal” star formation activity, vary smoothly as a function of stellar mass and SFR according to the calibration of the fundamental metallicity plane given in Mannucci et al. (2010; see also Lara-López et al. 2010). To compute the corresponding value of the conversion factor, M. Sargent et al. (2012, in preparation) assume a variation of $\alpha_{\text{CO}} \propto Z^{-1}$ as they find that this relation between metallicity and α_{CO} reproduces the faint-end slope of the $z = 0$ CO LF of Keres et al. (2003) best, under the set of assumptions just described.

The colored tracks in Figure 7(b) delineate the variations of α_{CO} with $\text{sSFR}/\langle\text{sSFR}\rangle_{\text{MS}}$ expected for galaxies in three bins of total stellar mass. Three regions can be clearly distinguished: (1) the *MS locus*, characterized by a gradual increase of α_{CO} with sSFR that is caused by the slight rise in metallicity predicted by the FMR; (2) the *SB region* at high $\text{sSFR}/\langle\text{sSFR}\rangle_{\text{MS}} \gg 4$, where the conversion factor, by construction, assumes a mass- and redshift-independent, constant value; and (3) a narrow *transition region* (spanning roughly $\text{sSFR}/\langle\text{sSFR}\rangle_{\text{MS}} \in [2, 4]$), where α_{CO} drops from an approximately MW-like conversion factor to the SB value. Note that, in contrast to the previous case, α_{CO} varies only slightly among MS galaxies. This weak dependence of α_{CO} on $\text{sSFR}/\text{sSFR}_{\text{MS}}$ introduces a step as we move from MS to SB systems. In the emerging picture, the majority of the star-forming population is dominated by either the MS or SB mode, and only a small fraction consists of “composite” star-forming galaxies hosting both normal and SB activities. For composite sources, the α_{CO} should be interpreted as a mass-weighted, average conversion factor that reflects the relative amount of the molecular gas reservoir that fuels star-forming sites experiencing burst-like and secular star formation events, respectively. Note also that variations with redshift (indicated by different colored lines in Figure 7(b)) are small for the limited range of stellar mass covered by our sample and would likely be indistinguishable within the natural scatter about the median trends plotted in the figure.

Both scenarios appear to be consistent with the data, leaving open the question of whether the transition from normal to SB galaxies is followed by a smooth or a step-like variation of α_{CO} . However, both scenarios agree in that α_{CO} should not vary much *within* the MS. Indeed, even for the case of continuous variation, the decrease of α_{CO} becomes statistically significant only for strongly starbursting systems, as Equation (9) indicates that α_{CO} would vary at most by a factor of ~ 2 within the full range of the MS, well within the observed scatter of the relation. Therefore, the average value $\alpha_{\text{CO}} \sim 5$, as derived in this study, can be regarded as representative for the whole population of MS galaxies at any redshift, with stellar masses $\geq 10^{10} M_{\odot}$. We remind the reader that because sSFR_{MS} increases with redshift as $(1+z)^{2.95}$, at least out to $z \approx 2.5$, galaxies with (U)LIRG-like luminosities can enter the MS at higher redshifts or at large stellar masses (e.g., Sargent et al. 2012). We stress that our analysis suggests that the α_{CO} of these systems, i.e., high- z MS

ULIRGs, is on average a factor of ~ 5 larger than that of local ULIRGs.

4.5. Comparison with Theoretical Predictions

The determination of the α_{CO} value has also been the focus of several theoretical studies. In particular, Narayanan et al. (2011) investigated the dependence of α_{CO} on the galactic environment in numerical simulations of disk galaxies and galaxy mergers and reported a relationship between α_{CO} and the CO surface brightness of a galaxy. Here, we compare our observationally constrained α_{CO} values with those predicted by their theoretical approach. According to Narayanan et al. (2011),

$$\alpha_{\text{CO}} = \frac{6.75 \times 10^{20} \langle W_{\text{CO}} \rangle^{-0.32}}{6.3 \times 10^{19} \times (Z/Z_{\odot})^{0.65}}, \quad (10)$$

where $\langle W_{\text{CO}} \rangle$ is the CO surface brightness of the galaxy in K km s^{-1} . According to Solomon & Vanden Bout (2005),

$$L'_{\text{CO}} = 23.5 \times \Omega_{\text{B}*S} D_L^2 I'_{\text{CO}} (1+z)^{-3}, \quad (11)$$

where L'_{CO} is measured in $\text{K km s}^{-1} \text{ pc}^2$, $\Omega_{\text{B}*S}$ is the solid angle of the source convolved with the telescope beam measured in arcsec^2 , and I'_{CO} is the observed integrated line intensity in K km s^{-1} . In the case of an infinitely good resolution, as assumed in Narayanan’s simulations, this becomes the solid angle subtended by the source. The CO line luminosity can also be expressed for a source of any size in terms of the total line flux:

$$L'_{\text{CO}} = 3.25 \times 10^7 S_{\text{CO}} \Delta v v_{\text{obs}}^{-2} D_L^2 (1+z)^{-3}, \quad (12)$$

where $S_{\text{CO}} \Delta v$ is the velocity integrated flux in Jy km s^{-1} . From Equations (11) and (12), and for the case of an infinitely good resolution, we derive

$$W_{\text{CO}} = 1.38 \times 10^6 \frac{4 \times v_{\text{obs}}^{-2}}{\pi (1+z) \theta^{-2}} \times S_{\text{CO}} \Delta v, \quad (13)$$

where v_{obs} is the observed frequency and θ is the size of the source in arcsec.¹⁷ For our sources we use, where possible, the CO sizes, and UV sizes when CO observations are too noisy to reliably measure the source extent. Using Equations (10) and (13), we then get an estimate of α_{CO} for each source in our sample according to the prescription of Narayanan et al. (2011), and in Figure 8 we compare them to the values derived based on our method. Although there seems to be a small systematic offset (on average by a factor of ~ 1.4) toward lower values for the theoretical approach, the overall agreement of the α_{CO} values is very good when one considers the large uncertainties and assumptions of the two independent methods. We stress that the derived $\langle W_{\text{CO}} \rangle$ and therefore the estimated α_{CO} values are very sensitive to the choice of the size indicator.

4.6. Implications for the Star Formation Activity of High- z MS Galaxies

While the sSFR probes the star formation mode of a galaxy only indirectly and from a statistical point of view, accurate measurements of its star formation efficiency,

¹⁷ We introduce a $(1+z)$ term here, not present in the original Narayanan et al. formula, which is required in order to make α_{CO} independent of redshift for fixed physical properties of the galaxies. Without that term the systematic difference between predicted and measured α_{CO} values would grow to a factor of two.

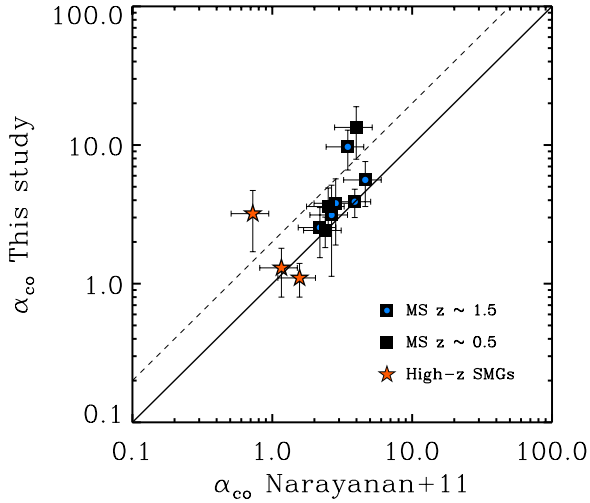


Figure 8. Comparison between the δ_{GDR} -inferred α_{CO} values for the galaxies in this study and those predicted by the theoretical approach of Narayanan et al. (2011). MS galaxies at $z \sim 0.5$ and $z \sim 1.5$ are shown with black squares and blue circles, respectively, while SMGs are depicted as orange stars. The solid line is the one-to-one relation and the dashed line its offset in y , by a factor of two.

(A color version of this figure is available in the online journal.)

$\text{SFE} = \text{SFR}/M_{\text{gas}}$, can provide more direct and reliable answers. With the robust α_{CO} estimates derived in this study, we can convert the CO measurements into M_{gas} and subsequently infer the SFE of galaxies in our sample. In what follows we use $\text{SFE} = \text{SFR}/M_{\text{gas}}$ and $\text{SFE} = L_{\text{IR}}/M_{\text{gas}}$ interchangeably, since SFR is linearly related to L_{IR} through $\text{SFR} = L_{\text{IR}} \times 10^{-10}$ (i.e., through the Kennicutt (1998) relation, calibrated for a Chabrier IMF).

We have so far established that even though there appears to be only small variation of α_{CO} among MS galaxies, the α_{CO} of high- z MS galaxies is similar to that of local disks with lower L_{IR} and is ~ 5 times larger than the average α_{CO} value observed for local ULIRGs. The direct implication of this finding is that for a given L_{CO} , one could expect a large variation in the amount of molecular gas for galaxies between MS and

SB galaxies. This also suggests that for a given L_{IR} (or equally, SFR), galaxies in the MS have lower SFEs, as compared to starbursting systems. Indeed, using the inferred α_{CO} values, we derive SFE estimates for each source in our sample and plot them against $\text{sSFR}/\text{sSFR}_{\text{MS}}$ in Figure 9(a). We supplement our sample with a compilation of local disks (Leroy et al. 2008), as well as with a sample of local ULIRGs (Solomon et al. 1997; Rodríguez Zaurín et al. 2010).

Although the actual dependence of SFE on $\text{sSFR}/\text{sSFR}_{\text{MS}}$ within the MS and the transition from MS to the SB regime will be discussed in detail in the next section, here we can derive some crucial results about the SFE of the two populations (MS and SB galaxies) by employing a simple, empirical relation between SFE and $\text{sSFR}/\text{sSFR}_{\text{MS}}$. Indeed, a linear regression fit and a Spearman's test to our high- z data (including SBs) yield a strong and statistically significant correlation ($\rho = 0.71$, p -value = 0.0012) between SFE and $\text{sSFR}/\text{sSFR}_{\text{MS}}$, with

$$\text{SFE} = (8.1 \pm 1.2) \times [\text{sSFR}/\text{sSFR}_{\text{MS}}]^{1.34 \pm 0.13}, \quad (14)$$

suggesting substantially higher SFEs for galaxies with enhanced sSFR (Figure 9(a)). For MS galaxies, we find an average $\langle \text{SFE} \rangle = (14 \pm 2) L_{\odot}/M_{\odot}$, corresponding to an average gas consumption timescale ($\tau_{\text{gas}} = M_{\text{gas}}/\text{SFR}$) of ~ 0.7 Gyr, indicative of long-lasting star formation activity. This is in direct contrast to the short-lived, merger-driven SB episodes observed in local ULIRGs, with an average $\langle \text{SFE} \rangle = 200 L_{\odot}/M_{\odot}$, ~ 12 times higher than that of MS galaxies. Since the majority of galaxies at any redshift are MS galaxies (e.g., Elbaz et al. 2011) and SB galaxies seem to play a minor role in the star formation density throughout the cosmic time (e.g., Rodighiero et al. 2011; Sargent et al. 2012), our results come to support the recently emerging picture of a secular, long-lasting star formation as the dominant mode of star formation in the history of the universe.

To ensure that our result is not an artifact of the assumed α_{CO} values, in Figure 10 we also plot the ratio of the direct observables, $L_{\text{IR}}/L'_{\text{CO}}$ versus the offset from the MS for the same set of objects, omitting any assumptions for α_{CO} . We find the two values to strongly correlate with $\rho = 0.79$ and a p -value

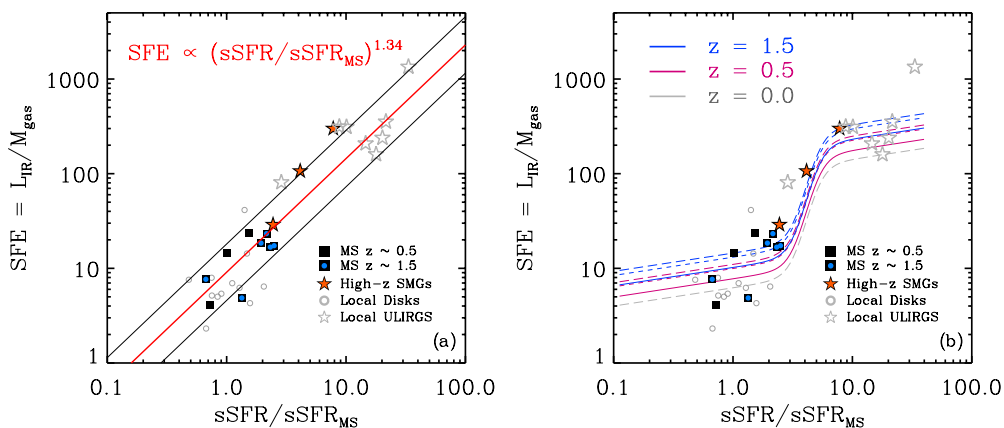


Figure 9. (a) Star formation efficiency, $\text{SFE} = L_{\text{IR}}/M_{\text{gas}}$, against the offset from the main sequence. Black squares and orange stars are the MS galaxies and the SMGs considered in this study. Empty gray circles are local normal galaxies (Leroy et al. 2008; Schruba et al. 2012), and gray stars depict local ULIRGs (Rodríguez et al. 2010; Solomon et al. 1997). For local ULIRGs, we have assumed $\alpha_{\text{CO}} = 0.8$. The red solid line depicts the best fit to the data with a slope of 1.34, while a Spearman's rank test indicates a tight correlation between the plotted quantities with $\rho = 0.71$. (b) Same as the left panel but for the case of a weak increase of SFE with $\text{sSFR}/\text{sSFR}_{\text{MS}}$ within the main sequence. Tracks show the dependence of SFE on $\text{sSFR}/\text{sSFR}_{\text{MS}}$ as expected for a slightly sublinear relation between M_{gas} and SFR and the relative importance of the starburst and main-sequence mode of star formation as a function of $\text{sSFR}/\text{sSFR}_{\text{MS}}$. Blue (purple), solid, dashed, and long-dashed lines correspond to $z = 1.5$ ($z = 0.5$) for $M_* = 1.0 \times 10^{10} M_{\odot}$, $5.0 \times 10^{10} M_{\odot}$, and $1.0 \times 10^{11} M_{\odot}$. The gray long-dashed line corresponds to $z = 0$ and $M_* = 1.0 \times 10^{11} M_{\odot}$.

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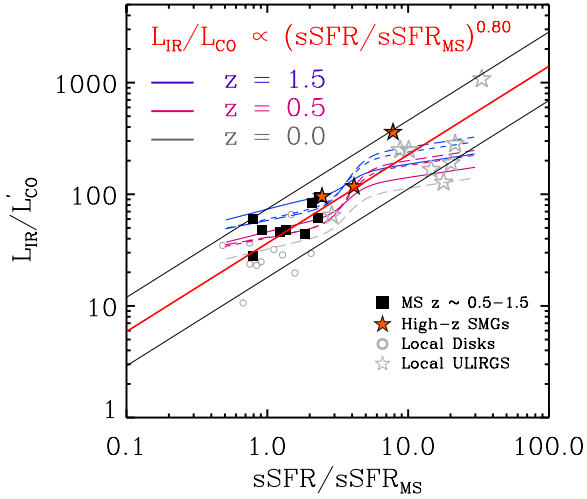


Figure 10. Ratio of direct observables, $L_{\text{IR}}/L'_{\text{CO}}$, against the offset from the main sequence for the same set of objects as in Figure 9. The red solid line is the best fit to the data, with a slope of 0.80. Colored tracks correspond to the scenario by Sargent et al. (2012), following the convention of Figure 9.

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of 3.4×10^{-6} and a functional relationship of

$$L_{\text{IR}}/L'_{\text{CO}} = 34.6(\pm 5.0) \times [\text{sSFR}/\text{sSFR}_{\text{MS}}]^{0.80 \pm 0.1}, \quad (15)$$

with MS galaxies exhibiting lower $L_{\text{IR}}/L'_{\text{CO}}$ values by a factor of ~ 4 . We note, however, that the absence of a well-defined sample of high- z SBs is striking. SMGs, which are frequently regarded as prototypical high- z SBs, have recently turned out to be more likely a mixed ensemble of objects, with a significant fraction of them exhibiting SFRs and SFEs typical of MS galaxies (Ivison et al. 2011; Rodighiero et al. 2011). Indeed, while we have only three SMGs in this study, we seem to face the same situation. Of the three SMGs considered here, only HSLW-01 appears to be a strong SB, with $\text{sSFR}/\text{sSFR}_{\text{MS}} \sim 10$ and $\text{SFE} \sim 300 L_{\odot}/M_{\odot}$. GN 20 is only marginally outside the MS regime, with $\text{sSFR}/\text{sSFR}_{\text{MS}} \sim 4$, although with high $\text{SFE} \sim 120 L_{\odot}/M_{\odot}$, while SMM-J2135 behaves like an MS galaxy with $\text{sSFR}/\text{sSFR}_{\text{MS}} \sim 2.5$ and $\text{SFE} \sim 30 L_{\odot}/M_{\odot}$, much lower than the SFE observed for local ULIRGs ($> 100 L_{\odot}/M_{\odot}$). Clearly a larger, objectively selected sample of high- z SBs is essential to improve this investigation.

5. VARIATIONS OF SFE WITHIN THE MAIN SEQUENCE

In the previous section, we demonstrated that the bulk of MS galaxies exhibit higher α_{CO} values and have lower SFEs than SB galaxies. Here, we will attempt to investigate possible variations of SFE within the MS, taking into account that the thickness, i.e., the spread of the $\text{SFR}-M_*$ correlation as traced by normally star-forming galaxies at any redshift, is not just an artifact produced by random noise, but a manifestation of the variation of the physical properties of the MS galaxies, such as color and clumpiness (e.g., Salmi et al. 2012; see also Elbaz et al. 2011). Since the actual quantity that drives a galaxy above or below the MS is yet unknown, we will consider two limiting scenarios, where the relative position of a galaxy with respect to the MS is driven by (1) variations in the gas fraction ($f_{\text{gas}} = M_{\text{gas}}/[M_{\text{gas}} + M_*]$, or equally in the gas to stellar mass ratio, M_{gas}/M_*) while the SFE remains roughly constant within the MS, or (2) variations in the SFE of MS galaxies, while f_{gas} remains constant, in order to explain the observed dispersion

in the $\text{SFR}-M_*$ plane. Indeed, in practice there are two ways that an MS galaxy could have higher SFR: either it has more raw material (M_{gas}) to produce stars, or for the same amount of M_{gas} it is more efficient at converting that gas into stars. The two scenarios have direct implications on the star formation law (SF law) in the galaxies. The first case implies the existence of a *global* $L_{\text{IR}}-M_{\text{gas}}$ relation that would apply to all MS galaxies, irrespective of their sSFR, like the one presented by Daddi et al. (2010b) and Genzel et al. (2010). On the other hand, the second scenario would imply *variations* of the SF law, with parallel $M_{\text{gas}}-L_{\text{IR}}$ relations with constant slope, but with a normalization factor that strongly increases with offset from the MS. While a combination of the two possibilities might also be plausible, we will consider the two limiting cases for simplicity.

5.1. Limiting Cases

5.1.1. Scenario I: A Global SF Law for MS Galaxies; f_{gas} as a Key Parameter

In this scenario, the physical parameter that drives the sSFR of an MS galaxy is the gas fraction, while the SFE remains roughly constant. In this case we have an SF law in the form

$$\log M_{\text{gas}} = \xi_{\text{gas}} \times \log \text{SFR} + C_1, \quad (16)$$

where $\xi_{\text{gas}} = 1$ would imply $M_{\text{gas}}/\text{SFR} = \text{constant}$. However, there is observational evidence that $\xi_{\text{gas}} \approx 0.8$, i.e., slightly lower than unity (e.g., Daddi et al. 2010a; Genzel et al. 2010; M. Sargent et al. 2012, in preparation), suggesting a very mild dependence of SFE from SFR (or from $\text{sSFR}/\text{sSFR}_{\text{MS}}$, for fixed stellar mass), with a slope of ≈ 0.2 . On the other hand, dividing Equation (16) by stellar mass indicates that M_{gas}/M_* would vary as a function of sSFR (or equally as a function of SFR at fixed stellar mass) with

$$\frac{M_{\text{gas}}}{M_*} \propto \left[\frac{\text{sSFR}}{\text{sSFR}_{\text{MS}}} \right]^{0.8}. \quad (17)$$

In Figure 9(b), we explore the variations of SFE with normalized sSFR for three representative bins of mass and redshift, as predicted by M. Sargent et al. (2012, in preparation), based on the framework described above. The two factors that contribute to the evolutionary tracks are (1) the observation that at fixed SFR (or L_{IR}) SBs display more than an order of magnitude higher SFE than that of “normal” galaxies (e.g., Daddi et al. 2010b; Genzel et al. 2010; this study), and (2) the fact that the dependence of SFR on M_{gas} is slightly supra-linear, such that SFE increases with L_{IR} even when the MS galaxies and SBs are considered individually (i.e., Equation (16)). Point (2) is reflected in the weak increase of SFE throughout the MS and SB regimes ($\text{sSFR}/\langle \text{sSFR} \rangle_{\text{MS}} < 2$ and $\text{sSFR}/\langle \text{sSFR} \rangle_{\text{MS}} > 4$, respectively), while the rapid rise in SFE in the transition region is the manifestation of point (1) above. Note that the “jump” in SFE, from the normal to the SB galaxies, is not forced by the assumption of a bimodal star formation activity but naturally results from the weak increase of SFE with $\text{sSFR}/\text{sSFR}_{\text{MS}}$ within the MS. Similar tracks are presented in Figure 10, considering $L_{\text{IR}}/L'_{\text{CO}}$ instead of $L_{\text{IR}}/M_{\text{gas}}$.

5.1.2. Scenario II: A Varying SF Law for MS Galaxies; SFE as a Key Parameter

This scenario assumes that f_{gas} for MS galaxies remains constant and that the physical parameter that dictates the position of the galaxy on the $\text{SFR}-M_*$ plane is the SFE. Since

$f_{\text{gas}} = \text{const}$, then expressing SFE as a function of $\text{sSFR}/\text{sSFR}_{\text{MS}}$, i.e., at fixed stellar mass, we have

$$\log \text{SFE} = \log(\text{SFR}) + C_2, \quad (18)$$

suggesting a linear dependence of SFE on $\text{sSFR}/\text{sSFR}_{\text{MS}}$, in reasonable agreement with the slope derived by a linear fit ($\xi_{\text{SFE}} = 1.34 \pm 0.13$, Equation (14)). Although a similar slope is found when the fit is redone for MS galaxies alone, excluding the SBs, a Spearman's test suggests that the correlation is statistically insignificant ($\rho = 0.58$, p -value = 0.13), leaving open the question of whether the trend is valid *within* the MS, or if it is driven solely by the SBs. A similar picture emerges when, instead of M_{gas} , we consider the directly observable quantity L'_{CO} (Figure 10). Again, in this case, excluding the SB data results in a statistically insignificant correlation. If indeed the SFE of MS galaxies follows such a steep increase as a function of $\text{sSFR}/\text{sSFR}_{\text{MS}}$, aside from the existence of parallel $M_{\text{gas}}-L_{\text{IR}}$ SF laws, it would also imply a smooth, continuous transition from MS to SB galaxies.

Both scenarios considered here appear to be consistent with our data, and we cannot formally distinguish between them based on these individual objects. However, as we will see in the next section, the shape of the SED, both for individually elected sources and for populations averaged via stacking, can provide more definite answers.

6. DISSECTING THE “THICKNESS” OF THE MAIN SEQUENCE

So far, we have seen that the high-quality SEDs offered by *Herschel* and millimeter continuum data can be used to reveal a strong dependence of the α_{CO} and SFE of a galaxy on its deviation from the MS (Equations (9) and (14)), highlighting significant differences between high- z MS galaxies and local ULIRGs, even though the former may have (U)LIRG-like luminosities and SFRs. The well-sampled SEDs considered in this study can provide the tools to further explore the implications of the two scenarios presented in the previous section.

We have argued that the relation $M_{\text{gas}}/M_{\text{dust}} \propto Z^{-1}$, observed in the local universe, holds at high z . A direct consequence of this assumption is that the ratio between the infrared luminosity and the dust mass of a galaxy at any redshift would be

$$\frac{L_{\text{IR}}}{M_{\text{dust}}} \propto \frac{L_{\text{IR}}}{M_{\text{gas}} \times Z} = \frac{\text{SFE}}{Z}, \quad (19)$$

with $L_{\text{IR}} \propto \text{SFR}$ for dusty galaxies where the extinction is large.¹⁸ Based on this relation, we can make some predictions for the different trends between $L_{\text{IR}}/M_{\text{dust}}$ and M_* and $\text{sSFR}/\text{sSFR}_{\text{MS}}$, for the two scenarios described above. Afterward, we will attempt to constrain the observational trend by stacking large samples of mass-selected high- z galaxies.

6.1. Trends in $L_{\text{IR}}/M_{\text{dust}}$ for $\text{SFE} \approx \text{Constant}$

For the case where f_{gas} varies within the MS (scenario I, Section 5.1.1), we have Equation (16) still holding. Also, using the $z \sim 2$ stellar mass—metallicity relation of Erb et al. (2006), we get

$$\log Z = \xi_z \times \log M_* + C_3, \quad (20)$$

¹⁸ In detail, $L_{\text{IR}} \propto (\text{SFR}_{\text{tot}} - \text{SFR}_{\text{UV}})$, with SFR_{UV} becoming significant in the case of low extinction, hence typically at very low galaxy masses and metallicities or at high redshifts.

with $\xi_z \sim 0.15$ for a stellar mass range of $10 \leq \log(M_*/M_\odot) \leq 11$. Finally, from the $\text{SFR}-M_*$ relation, we have

$$\log \text{SFR} = \xi_{\text{ms}} \times \log M_* + C_4, \quad (21)$$

with $\xi_{\text{ms}} \approx 0.80$. Combining the above relations yields

$$\log \frac{\text{SFE}}{Z} = (\xi_{\text{ms}} - \xi_{\text{gas}} * \xi_{\text{ms}} - \xi_z) \times \log M_* + C_5. \quad (22)$$

Substituting the values quoted above for the various ξ coefficients very nearly cancels out any dependence on $\log M_*$, giving

$$\log \frac{L_{\text{IR}}}{M_{\text{dust}}} \propto \log \frac{\text{SFE}}{Z} \approx C_5, \quad (23)$$

i.e., a negligible dependence of the dust-mass-weighted luminosity $L_{\text{IR}}/M_{\text{dust}}$ with M_* . Expressing SFE as a function of sSFR , i.e., as a function of SFR for fixed stellar mass (and therefore metallicity), yields

$$\log \frac{L_{\text{IR}}}{M_{\text{dust}}} = \log \text{SFE} = (1 - \xi_{\text{gas}}) \times \log \text{SFR} + C_1, \quad (24)$$

suggesting a mild dependence of $L_{\text{IR}}/M_{\text{dust}}$ with sSFR , with a slope of ~ 0.2 .

6.2. Trends in $L_{\text{IR}}/M_{\text{dust}}$ for $f_{\text{gas}} \approx \text{Constant}$

In the case where f_{gas} is constant among MS galaxies (scenario II, Section 5.1.2), where the thickness of the MS is the result of a strongly varying SFE (or equally, varying SF law), we have

$$\log \frac{L_{\text{IR}}}{M_{\text{dust}}} = \log \text{SFE} + C_6 = \log \text{SFR} + C_7 \quad (25)$$

since M_{gas} is constant at a fixed stellar mass and f_{gas} . This suggests a strong dependence of $L_{\text{IR}}/M_{\text{dust}}$ on $\text{sSFR}/\text{sSFR}_{\text{MS}}$. Note that $L_{\text{IR}}/M_{\text{dust}}$ is not expected to vary with M_* , as was also the case for the previous scenario (Equation (23)).

Summarizing the analytical predictions, the two scenarios result in two distinct behaviors of $L_{\text{IR}}/M_{\text{dust}}$ and f_{gas} as a function of $\text{sSFR}/\text{sSFR}_{\text{MS}}$. In the case of a weak increase of SFE within the MS ($\text{SFE} \approx \text{const}$, or equally, of a global SF law for MS galaxies), we expect a variation of f_{gas} (Equation (17)), while $L_{\text{IR}}/M_{\text{dust}}$ remains roughly constant within the MS (Equation (25)). The opposite trends are expected for the case where f_{gas} remains constant (or equally, of a varying SF law), i.e., a steep increase of SFE within the MS and a linear increase of $L_{\text{IR}}/M_{\text{dust}}$ with $\text{sSFR}/\text{sSFR}_{\text{MS}}$ (Equation (26)). We note that both scenarios predict only weak dependence of $L_{\text{IR}}/M_{\text{dust}}$ with M_* . Furthermore, the physical meaning of $L_{\text{IR}}/M_{\text{dust}}$ is the luminosity emitted per unit of dust mass, or the strength of the mean radiation field heating the dust, and could serve as a rough proxy of the effective dust temperature. Indeed, since, $L_{\text{IR}} \propto \sigma T_d^4$, two sources with the same $L_{\text{IR}}/M_{\text{dust}}$ should have similar T_d . Similarly, for a given M_{dust} , higher L_{IR} indicates higher T_d . Therefore, the above analysis also suggests a strong variation of the SED shape of the galaxies within the MS for the scenario where $f_{\text{gas}} \approx \text{constant}$ but only very little, if any, change in the shape of the SED for the case where $\text{SFE} \approx \text{constant}$.

6.3. $L_{\text{IR}}/M_{\text{dust}}$ and Gas Fractions in MS Galaxies

Using the stacked samples of $z \sim 2$ MS galaxies in three stellar mass and four sSFR bins, described in Section 2, we can investigate what trends, if any, are present between

Table 4
Derived Properties for Stacked Sub-samples of $z \sim 2$ MS Galaxies

Stack ^a	$\log L_{\text{IR}}$ (L_{\odot})	$\log M_{\text{dust}}$ (M_{\odot})	$\log \langle M_{*} \rangle$ (M_{\odot})	IR8 ^b	Z _{pp04}	$\log M_{\text{gas}}^c$ (M_{\odot})
sSFR1	11.44 ± 0.05	8.18 ± 0.11	10.09	4.5 ± 0.7	8.44	10.28 ± 0.19
sSFR2	11.49 ± 0.05	8.26 ± 0.09	10.04	4.7 ± 0.7	8.41	10.38 ± 0.13
sSFR3	11.58 ± 0.08	8.32 ± 0.09	10.04	5.2 ± 0.1	8.41	10.44 ± 0.16
sSFR4	11.80 ± 0.06	8.51 ± 0.09	10.17	5.8 ± 1.0	8.43	10.61 ± 0.13
mass1	11.29 ± 0.06	8.08 ± 0.10	9.84	4.9 ± 0.7	8.35	10.34 ± 0.15
mass2	11.78 ± 0.06	8.52 ± 0.08	10.33	5.0 ± 0.8	8.48	10.64 ± 0.13
mass3	12.05 ± 0.05	8.83 ± 0.08	10.80	4.9 ± 0.7	8.65	10.80 ± 0.13
Total	11.55 ± 0.06	8.27 ± 0.11	10.10	5.1 ± 0.5	8.40	10.45 ± 0.11
Total-z1	11.21 ± 0.09	8.14 ± 0.13	10.44	4.5 ± 0.6	8.62	10.04 ± 0.12

Notes.

^a The stacking sub-samples in sSFR and stellar mass bins are given in increasing order of $\langle \text{sSFR} \rangle / \text{sSFR}_{\text{MS}}$ and $\langle M_{*} \rangle$. The last line corresponds to the total stacked sample of $z \sim 1$ MS galaxies.

^b Defined as L_{IR}/L_8 , where L_8 is measured from the stacked $24 \mu\text{m}$ flux.

^c Estimated through the $\delta_{\text{GDR}}-Z$ relation based on the derived M_{dust} and the assumed Z_{pp04} .

$L_{\text{IR}}/M_{\text{dust}}-M_{*}$ and $L_{\text{IR}}/M_{\text{dust}}-\text{sSFR}/\text{sSFR}_{\text{MS}}$. To derive the far-IR properties of the stacked samples, we followed the same SED fitting procedure used for the individually detected sources. However, this time we take into account the redshift distribution of the stacked sources, to account for artificial SED broadening in the far-IR and smearing of the spectral features in the mid-IR regime. Namely, we construct the whole set of DL07 models at various redshifts and create an average SED at the median redshift of the sources considered in the stack by co-adding the model SEDs at each redshift, weighted by the redshift distribution of stacked sources. The two methods return far-IR luminosities that are in good agreement, although not accounting for the redshift distribution of the stacked sources results in higher $L_{\text{IR}}/M_{\text{dust}}$ values. This is expected as in this case the artificial broadening drives the fit, erroneously, to higher γ values, i.e., higher contribution of the PDR component, that result in lower M_{dust} for a given L_{IR} . We also validate the reliability of the inferred dust masses of the stacked samples against a possible artificial broadening of the SEDs from the dispersion of the shape of the SED of the sources included in the stacking. Namely, based on the value of $\langle U \rangle$ derived from the best fit to the stacked data, we generated 1000 artificial SEDs, adopting a scatter of 0.2 dex in $\langle U \rangle$, and assigned to each of them a redshift based on the redshift distribution of the original sample. Then, we produced an average SED that we fit in the same manner as the original data. We find that the derived $\langle U \rangle$ value for the simulated data is in very good agreement with the one obtained for the real data. The best-fit models for the various sSFR and stellar mass bins are shown in Figure 11, along with the stacked photometric points, while the inferred parameters are presented in Table 4. We note that for every sSFR bin, the derived L_{IR} implies an average SFR, and subsequently an average sSFR, that is very close to the initial corrected-for-extinction, UV-based sSFR estimate. This is also the first time that *Herschel* data provide evidence that the thickness of the MS at $z = 2$ is real and not due to scatter arising from uncertainties in the derivation of SFR.

As a reference point, we also consider the large compilation of normal galaxies in the nearby universe ($\langle z \rangle \approx 0.05$) and local ULIRGs by da Cunha et al. (2010a, 2010b). The dust mass estimates in these studies are derived based on a two-component fit for warm and cold dust, known to give results consistent with

those from the DL07 models (Magrini et al. 2011). Therefore, a direct comparison with our sample is meaningful after applying a correction factor of ~ 1.7 to the dust masses of the da Cunha et al. (2010a, 2010b) sample, to account for the different κ value adopted in their study.

Figure 11 reveals a remarkable similarity in the average SEDs of $z \sim 2$ MS galaxies for different sSFR bins, indicating a very small variation of the SED shape of the galaxies within the MS. This is further manifested by the weak dependence of $L_{\text{IR}}/M_{\text{dust}}$ with sSFR/sSFR_{MS} (inset panel), both for the $z \sim 2$ sample and also for the local, normal galaxies (slope of 0.11 ± 0.04). We reach similar conclusions when considering the SEDs for different stellar mass bins: the shape of the SED and the value of $L_{\text{IR}}/M_{\text{dust}}$ for both $z \sim 2$ and $z \sim 0$ MS galaxies appear to be independent of the stellar mass. The observed trends between $L_{\text{IR}}/M_{\text{dust}}$ versus sSFR/sSFR_{MS} and $L_{\text{IR}}/M_{\text{dust}}$ versus M_{*} are in striking agreement with those derived by our analytical approach, favoring a small variation of SFE within the MS, and therefore (1) the existence of a global SF law for MS galaxies and (2) a step-like dependence of SFE with sSFR/sSFR_{MS}. Indeed, the scenario of continuously increasing SFE would imply a considerable increase of $L_{\text{IR}}/M_{\text{dust}}$ (shown in the inset panel of Figure 11 (top) with a dashed line) and a noticeable change of SED shape of galaxies within the MS, something that is not supported by our data.

Our data can also be used to infer the dependence of f_{gas} on sSFR and M_{*} . Namely, from the derived M_{dust} and Z values, we can use the $\delta_{\text{GDR}}-Z$ relation to estimate M_{gas} and subsequently f_{gas} or M_{gas}/M_{*} . In Figure 12, we plot the derived M_{gas}/M_{*} as a function of sSFR/sSFR_{MS} and M_{*} for the normal galaxies at $z \sim 2.0$ and $z \sim 0$. We find a clear trend of increasing M_{gas}/M_{*} with increasing sSFR for both samples, with

$$\frac{M_{\text{gas}}}{M_{*}} = (2.05 \pm 0.32) \times \left[\frac{\text{sSFR}}{\text{sSFR}_{\text{MS}}} \right]^{0.87 \pm 0.15}, \quad (26)$$

very close to the slope derived in Equation (17). This result further supports that it is variations of f_{gas} , rather than variations of SFE, that are responsible for the thickness of the SFR- M_{*} relation at any redshift. We also reveal a clear trend of decreasing f_{gas} with increasing stellar mass, with

$$\log \left(\frac{M_{\text{gas}}}{M_{*}} \right) = (5.63 \pm 0.39) - (0.51 \pm 0.10) \times \log(M_{*}), [M_{*} \text{ in } M_{\odot}], \quad (27)$$

in agreement with various studies that predict a similar behavior (e.g., Daddi et al. 2010a; Saintonge et al. 2011; Davé et al. 2012; Popping et al. 2012; Fu et al. 2012). Note that these trends are due to the sublinear slopes of the SFR versus M_{*} and M_{gas} versus SFR relations (see Daddi et al. 2010a).

We recall that the M_{gas} derived with the δ_{GDR} method traces the total gas of a galaxy, i.e., $M_{\text{H}_2} + M_{\text{H I}}$. As we have discussed above, in our analysis we have assumed that H_2 dominates the gas mass of relatively massive ($M_{*} > 10^{10} M_{\odot}$) high- z galaxies. An indirect way to investigate this assumption is to compare the inferred M_{gas} and L_{IR} of the $z \sim 2$ sample to the $L_{\text{IR}}-M_{\text{H}_2}$ SF law for MS galaxies as derived by Daddi et al. (2010a), based on the dynamical properties of the individually detected BzK galaxies considered in our study. If $M_{\text{H I}}$ contributed significantly to the total gas mass, then the galaxies would appear to show an excess in M_{H_2} with respect to L_{IR} . This comparison, for various subsets of our $z \sim 2$ sample, is shown in Figure 13. The very good

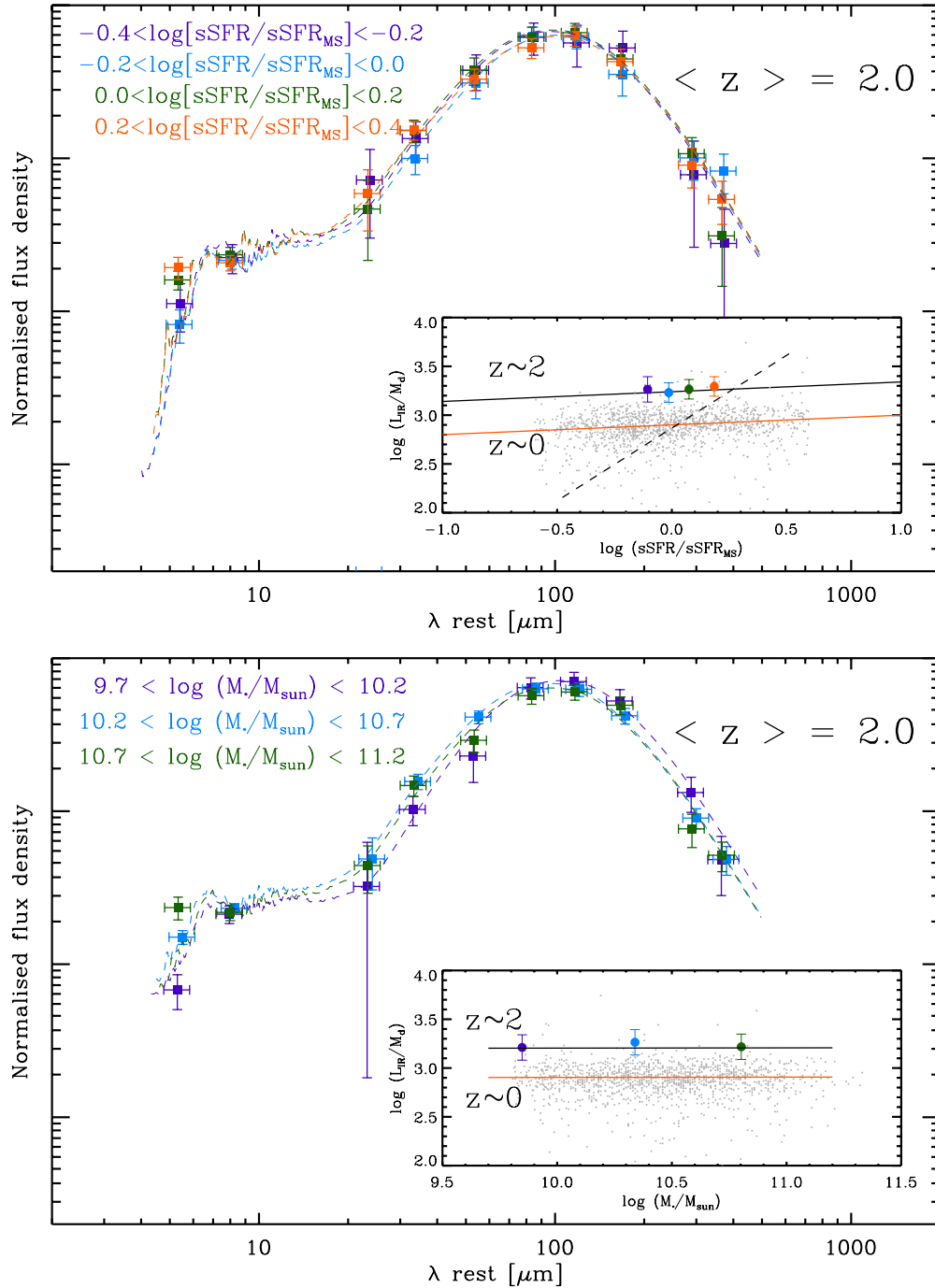


Figure 11. Top: observed average SEDs of $z \sim 2.0$ main-sequence galaxies in four sSFR bins, derived by stacking and overlaid with the best-fit Draine & Li (2007) models. Symbols are color-coded based on the four sSFR bins. The inset panel shows the derived L_{IR}/M_{dust} as a function of the offset from the main sequence for the $z \sim 2$ sample (colored squares), as well as for a set of normal galaxies in the local universe by da Cunha et al. (2010a; gray dots). For the $z \sim 2$ sample, the sSFR/sSFR_{MS} is derived based on *Herschel* measurements. The red solid line is the best fit to the local data, with a slope of 0.1. The black solid line shows the linear relation with a 0.5 dex offset. The black dashed line shows the expected trend for the case of a steep and continuous increase of SFE with sSFR/sSFR_{MS}. Bottom: observed average SEDs of $z \sim 2.0$ main-sequence galaxies in three stellar mass bins, derived by stacking and overlaid with the best-fit Draine & Li (2007) models. Symbols are color-coded based on the three stellar mass bins. The inset panel shows derived L_{IR}/M_{dust} as a function of the stellar mass for the $z \sim 2$ sample (colored circles) and for the same set of $z \sim 0$ normal galaxies as in the top panel.

(A color version of this figure is available in the online journal.)

agreement between the estimated M_{gas} and the SF law seems to validate our assumption (i.e., negligible contribution from H I), at least for the stellar mass range considered in this study. Indeed, our M_{dust} measurements are (obviously) luminosity weighted and thus effectively SFR weighted. Similarly, the metallicity estimates that we adopt from the literature are luminosity/SFR weighted as well, so it is reasonable that our final estimates are

most sensitive to the gas connected to the ongoing SFRs, i.e., the molecular gas.

7. THE EVOLUTION OF L_{IR}/M_{dust} IN MS GALAXIES

Aside from the similar trend of a weak increase of L_{IR}/M_{dust} with sSFR for $z \sim 2$ and $z \sim 0$ normal galaxies, Figure 11

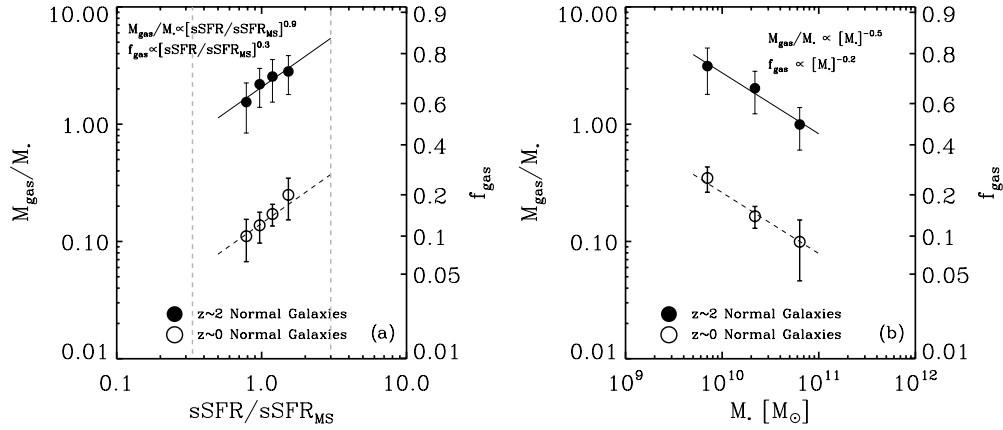


Figure 12. (a) Gas to stellar mass ratios (and gas fractions) as a function of deviation from the main sequence for the stacked sample of $z \sim 2.0$ (filled circles) and the mean values of $z \sim 0$ normal galaxies. Both samples are consistent with $M_{\text{gas}}/M_* \propto [\text{sSFR}/\text{sSFR}_{\text{MS}}]^{0.9}$, suggesting a strong increase of M_{gas}/M_* (and f_{gas}) with increasing sSFR at a given redshift. The solid black line is the best fit to the $z \sim 2$ data, and the dashed line has the same slope, normalized to the local sample. The gray horizontal lines define the region of MS galaxies. (b) Gas-to-stellar-mass ratios (and gas fractions) as a function of stellar mass for the same sample as in the left panel. The data suggest a decrease of M_{gas}/M_* with increasing M_* with $M_{\text{gas}}/M_* \propto M_*^{-0.5}$.

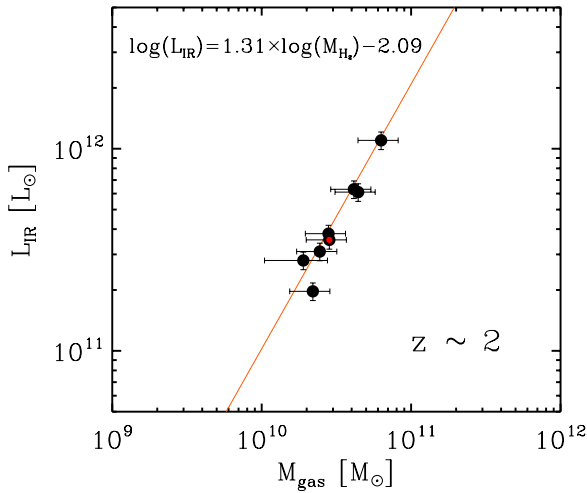


Figure 13. L_{IR} vs. M_{gas} for various stacked subsets in sSFR and M_* bins (black circles), as well as of the total sample (black circle with red dot) of $z \sim 2$ normal galaxies. The line depicts the $L_{\text{IR}}-M_{\text{H}_2}$ star formation law of local and high- z disk galaxies presented by Daddi et al. (2010b).

(A color version of this figure is available in the online journal.)

implies that the shape of the SED of MS galaxies at a given redshift, as traced by $L_{\text{IR}}/M_{\text{dust}}$, is not expected to vary significantly with increasing L_{IR} (i.e., SFR). Moreover, normal galaxies at $z \sim 2$ appear to exhibit systematically higher values of $L_{\text{IR}}/M_{\text{dust}}$ than their local counterparts, suggesting a possible trend of $L_{\text{IR}}/M_{\text{dust}}$ with cosmic time. To explore this further, we enhance our data set by performing SED fitting to the mean SED of MS galaxies at $z \sim 1$ derived through the stacking procedure described in Section 2. The stacked data points and best-fit models for the $z \sim 1$ and $z \sim 2$ MS galaxies are shown in Figure 14. The final sample available for our analysis consists of $z \sim 0$ normal galaxies from da Cunha et al. (2010a) and Draine et al. (2007), local ULIRGs from da Cunha et al. (2010b), individually detected MS galaxies at $z \sim 0.5$ and $z \sim 1.5$, mean SEDs of MS galaxies at $z \sim 1$ and $z \sim 2$, and SMGs at various redshifts. We also recall that $L_{\text{IR}}/M_{\text{dust}}$ is proportional to the mean radiation field $\langle U \rangle$ in the DL07 models (Equation (4)). Using the derived $\langle U \rangle$, L_{IR} , and M_{dust} values for our individual sources

and for the stacked samples, we find an average¹⁹ scaling factor between the two quantities of $P_0 \approx 125$.

In Figure 15 (left), we plot M_{dust} as a function of L_{IR} for the whole set of sources described above. Focusing at first on the local samples, we see that at $z \sim 0$, normal galaxies follow a tight relation with a slope close to but not equal to unity, ($\xi_{\text{ml}} = 0.95$), possibly mirroring the $L_{\text{IR}}-T_{\text{d}}$ relation observed both in the local and in the high- z universe (e.g., Hwang et al. 2010). However, we notice that this is a very mild increase of $L_{\text{IR}}/M_{\text{dust}}$. Indeed, the $L_{\text{IR}}/M_{\text{dust}}$ of the whole sample of the local normal galaxies exhibits a Gaussian distribution with a mean value of $\langle \log(L_{\text{IR}}/M_{\text{dust}}) \rangle = 2.89$ and a dispersion of 0.15 dex. To further examine whether sources with higher L_{IR} tend to have significantly higher $L_{\text{IR}}/M_{\text{dust}}$, we split the sample into two luminosity bins, $L_{\text{IR}} > 10^{11} L_{\odot}$ and $L_{\text{IR}} < 10^{11} L_{\odot}$, and find that the two sub-samples follow almost identical distributions (Figure 15, left, inset panel). In contrast, local ULIRGs are strong outliers from the $M_{\text{dust}}-L_{\text{IR}}$ relation formed by normal galaxies, with significantly higher $L_{\text{IR}}/M_{\text{dust}}$ values, indicative of their warmer ISM. The IRAS selection for the normal galaxies considered here could, in principle, introduce a bias toward warmer sources and miss cooler sources whose SEDs peak at longer wavelengths. Recent *Herschel* observations of local galaxies seem to confirm this, revealing a population of normal galaxies in the local universe that are systematically colder than the IRAS-selected sample (e.g., Smith et al. 2012). However, while the *Herschel*-selected galaxies would increase the scatter and shift the mean of $L_{\text{IR}}/M_{\text{dust}}$ distribution toward a lower value, they are also found to follow a $L_{\text{IR}}-M_{\text{dust}}$ relation with a slope close to unity, leaving the overall picture described above unaffected. At $z = 0$ the ULIRGs have an order of magnitude larger $L_{\text{IR}}/M_{\text{dust}}$ than normal (spiral) galaxies, consistent with the fact that they have a much higher SFE.

Moving to the high- z samples of MS galaxies, we notice a small deviation from the local relation, exhibiting on average higher $L_{\text{IR}}/M_{\text{dust}}$ values. Having already seen that we do not expect large variations of $L_{\text{IR}}/M_{\text{dust}}$ within MS galaxies at the same redshift, this indicates a small change in the shape of the SEDs of MS galaxies toward stronger radiation fields as we move back in cosmic time. This is clearly depicted in Figure 15

¹⁹ There is a small scatter ($< 5\%$) in the derived average scaling factor due to our definition of L_{IR} as $L_{8-1000 \mu\text{m}}$ instead of $L_{\text{IR}} = L_{0-\infty}$.

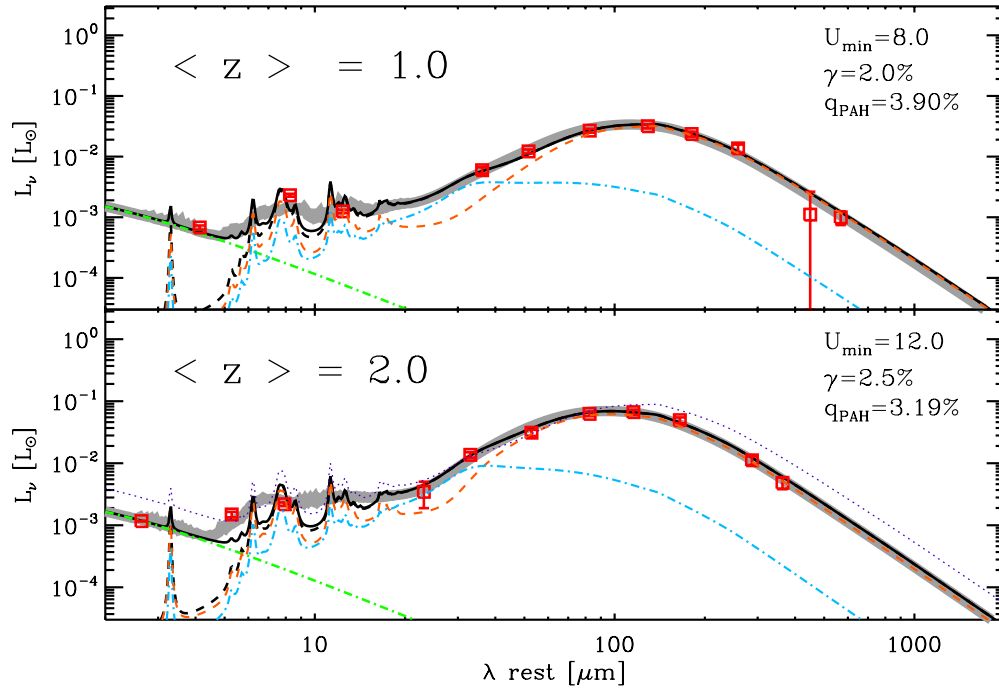


Figure 14. Observed average SEDs of main-sequence galaxies at $z \sim 1.0$ (top) and $z \sim 2.0$ (bottom) derived by stacking and overlaid with the best-fit Draine & Li (2007) models taking into account the redshift distribution of the stacked sources (gray solid line) and assuming the median redshift of each sample (solid black line). The black dashed line is the DL07 model without the stellar component that is depicted with a green dot-dashed line. Orange dashed and cyan dot-dashed lines show separate contributions of starlight and emission from dust heated by $U = U_{\min}$ (diffuse ISM component) and dust heated by $U_{\min} < U < U_{\max}$ (“PDR” component), respectively. The fitted parameters from the best-fit Draine & Li (2007) model fits are listed within each panel. For comparison, the best-fit SED of the $z \sim 1.0$ is also shown in the bottom panel with a blue dotted line.

(A color version of this figure is available in the online journal.)

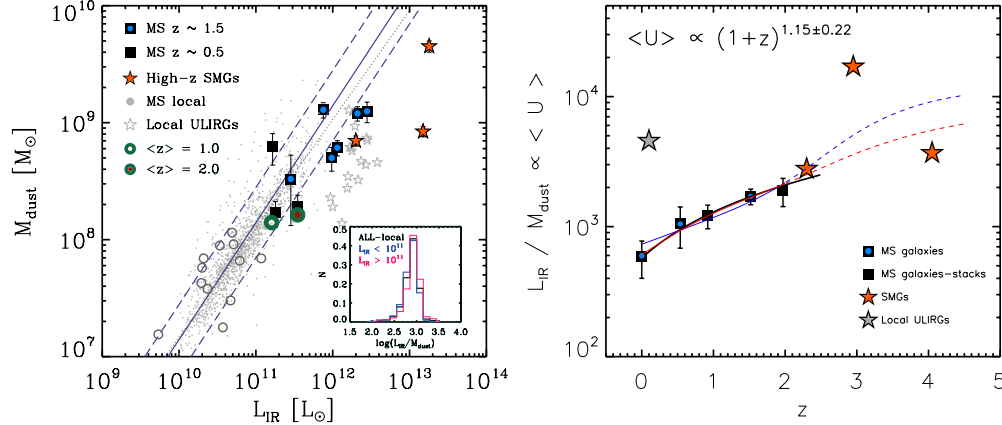


Figure 15. Left: dust mass as a function of infrared luminosity for local normal galaxies from the sample of da Cunha et al. (2010a) and the SINGS sample of Draine et al. 2007 (gray points and circles, respectively), local ULIRGs from da Cunha et al. 2010b (gray stars), individually detected MS galaxies at $z \sim 0.5$ (black squares) and $z \sim 1.5$ (black squares with blue circle), stacked MS galaxies at $z \sim 1.0$ (empty green circle) and $z \sim 2.0$ (filled green circle), and high- z SMGs (orange stars). The solid line corresponds to a linear relation between M_{dust} and L_{IR} , consistent with the data for local normal galaxies, although the best fit yields a slope of 0.95 (gray dotted line). The dashed lines show the linear relation with a ± 0.3 dex offset. Right: evolution of the mean radiation field $\langle U \rangle \propto L_{\text{IR}}/M_{\text{dust}}$ as a function of redshift. Black squares with blue circles depict individually detected normal star-forming galaxies at various redshifts. At $z \sim 0$ we use the average value as derived based on the samples of Draine et al. (2007), da Cunha et al. (2010a), and Dale et al. (2012), while at high z the median values from the individually detected sources at $z \sim 0.5$ and at $z \sim 1.5$. Black squares represent the stacking results at $z \sim 1$ and $z \sim 2$. Orange stars represent high- z SMGs considered in the study, while the gray star denotes the position of the local ULIRGs based on data from da Cunha et al. (2010b). The black solid line is the best fit to the MS galaxies, yielding a relation of $\langle U \rangle \propto (1+z)^{1.15}$. The blue and red solid lines show the expected evolution of SFE/Z with redshift for the case of $M_* = 1 \times 10^{10} M_{\odot}$ and $M_* = 5.0 \times 10^{10} M_{\odot}$, respectively, highlighting a co-evolution between SFE/Z and $\langle U \rangle$.

(A color version of this figure is available in the online journal.)

(right), where we plot $L_{\text{IR}}/M_{\text{dust}}$, or equally $\langle U \rangle$, as a function of redshift, for our samples, along with that of local galaxies. Our data suggest an increase of $\langle U \rangle \propto (1+z)^{1.15}$ for MS galaxies, pointing also toward an increase in their T_d with look-back time. This is not to be confused with the general conception that

ULIRGs tend to get colder at higher redshifts. Indeed, when comparing high- z MS ULIRGs to local galaxies of comparable L_{IR} (i.e., (U)LIRGs), the latter have much larger $L_{\text{IR}}/M_{\text{dust}}$ values, indicative of a much stronger starlight intensity field and a much warmer ISM, in line with recent studies that find

distant ULIRGs to be colder than their local counterparts (e.g., Symeonidis et al. 2009; Hwang et al. 2010; Magdis et al. 2010a; Muzzin et al. 2010). We also note that the evolution of T_d with redshift is directly demonstrated by the comparison of SEDs of the $z \sim 2$ and $z \sim 1$ samples, with the latter peaking at a longer wavelength. Since our stacks consist of galaxies with photometric redshift too, we also explored the possibility that the difference in the derived $\langle U \rangle$ arises from a systematic bias in the redshift distribution of the stacked samples. However, we find that for the two samples to peak at the same wavelength, this bias should be $\Delta z \approx 0.35$, which is unlikely given that the systematics in the derived photometric redshifts is $\Delta z \ll 0.1$ (e.g., Grazian et al. 2006; Santini et al. 2009; M. Pannella et al. 2012, in preparation).

As we have seen in Equation (19), the dust-weighted luminosity (or mean radiation field) is directly proportional to SFE/Z . It is easy to show how a similar evolution with redshift of SFE/Z can be expected based on a simple analytical approach. Two trends would drive the evolution of SFE/Z . One is the evolution (decrease) of metallicity at given stellar mass ($C_Z(z)$) derived by the mass–metallicity relation at various redshifts (Tremonti et al. (2004) for $z = 0$; Savaglio et al. (2005) for $z = 0.5$; Erb et al. (2006) for $z = 2$; Sommariva et al. (2012) for $z = 3$). The other is the evolution of the normalization of the $sSFR_{MS}$ at fixed stellar mass ($C_{MS}(z)$), which scales as $(1+z)^{2.8}$. At fixed stellar mass, we have

$$\log \frac{SFE}{Z}(z) = C + (1 - \xi_{gas}) \times C_{MS}(z) + C_Z(z), \quad (28)$$

and the emerging trend of SFE with redshift for the case of $M_* = 1 \times 10^{10} M_\odot$ and $M_* = 5.0 \times 10^{10} M_\odot$ is shown in Figure 15 (right), highlighting the striking agreement between the observed and the predicted trends. We stress that the metallicity evolution is mapped up to $z \sim 3$, so the values beyond this redshift are based on extrapolation. However, at very low metallicities, the SFR and L_{IR} could deviate from their linear relation, with L_{IR} tracing only a small fraction of the total star formation activity as dust attenuation becomes small and the directly visible UV emission becomes significant. In that scenario, we would expect some flattening of the SFE evolution beyond $z \sim 2$. In any case, we conclude that the observed increase of $\langle U \rangle$ with redshift up to $z \sim 2.0$ is in excellent agreement with the expectations based on our analytical approach. We stress that the observed increase of $\langle U \rangle$ with redshift is in line with both alternative scenarios, i.e., a weak and strong dependence of SFE on $sSFR/sSFR_{MS}$ for galaxies within the MS.

7.1. Template SEDs of MS Galaxies

We have seen that MS galaxies at a given redshift tend to have uniform radiation fields, parameterized by L_{IR}/M_{dust} , and an overall small variation in shape of their SED. We also presented evidence that the mean radiation field of MS galaxies increases with redshift as $\sim (1+z)^{1.15}$. This indicates that we could build template SEDs of MS galaxies at different redshifts. In the DL07 models, the mean radiation field $\langle U \rangle$ is an interplay between γ , which is the fraction of dust emission arising from PDRs, and U_{min} , which is the radiation field heating the diffuse ISM. We stress that the same $\langle U \rangle$ could arise from a different combination of γ and U_{min} and it does not monotonically define the shape of the SED. Although our sample is not sufficiently large to break this degeneracy, we can use the mean $\langle U \rangle$ values at each

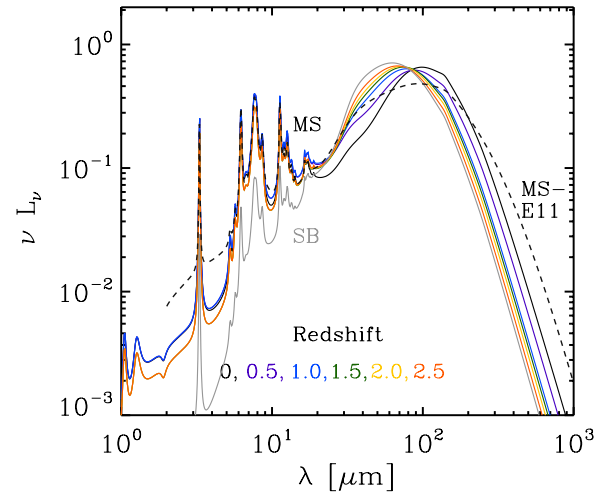


Figure 16. Template SEDs of MS galaxies at various redshifts built based on DL07 models and the evolution of $\langle U \rangle$ with cosmic time as $(1+z)^{1.15}$. The templates assume no evolution of the γ parameter in the DL07, i.e., the fractional contribution of the PDRs to the total IR emission of a galaxy and a small evolution of the q_{PAH} beyond $z \sim 2.0$, as indicated from our data. The templates are color-coded based on their redshift and normalized to $1 L_\odot$. For starburst galaxies, we show the best-fit template of GN 20 (gray line). The black dashed line shows the MS template SED of Elbaz et al. (2011).

(A color version of this figure is available in the online journal.)

redshift to construct template SEDs of MS galaxies, under the assumption that γ does not change significantly with time. We adopt a constant $\gamma = 0.02$, similar to that reported for local galaxies by Dale et al. (2012) and Draine et al. (2007). Indeed, if we were to reproduce the same $\langle U \rangle$ with higher γ values, then the shape of the SED would become unphysically flat close to the peak. Also, the galaxies in our sample have a mean γ very close to that value, so it seems like a valid simplification. Then, using the relation between $\langle U \rangle$ and redshift derived in the previous section, we built template SEDs of MS galaxies for a grid of redshifts up to $z = 2.5$ using the DL07 models. Beyond $z > 2.5$, we assume a flattening of the evolution of $\langle U \rangle$, similar to that observed for the $sSFR$ (e.g., González et al. 2010). For the remaining free parameter, q_{PAH} , we adopt the mean value of 3.19% up to redshift $z \sim 1.5$ and $q_{PAH} = 2.50\%$ at $z > 1.5$ as indicated by our data. The resulting MS SEDs are shown in Figure 16.

We note that the overall philosophy is very similar to that of Elbaz et al. (2011), who presented a single template for MS galaxies, with a unique far-IR-to-mid-IR luminosity ratio, IR8, at all redshifts up to $z > 2$ and a single template for starbursting systems with a significantly higher value of IR8. Here, we extend this approach but introduce some evolution of the SEDs of MS galaxies, following the increase of $\langle U \rangle$ with redshift. Our templates result in IR8 values that also mildly increase from $IR8 \sim 4.0$ at $z = 0$ to $IR8 \sim 6.0$ at $z > 2$, in agreement with Elbaz et al. (2011; D. Elbaz et al. 2012, in preparation) and with Reddy et al. (2012). Similar to Elbaz et al. (2011), for SB galaxies, we show here a unique template, using the best-fit SED of GN 20. Despite the simple and straightforward nature of these templates, we note that Béthermin et al. (2012a) find that they manage to reproduce recent *Herschel* source counts (e.g., Berta et al. 2011; Béthermin et al. 2012a), including counts measured in redshift slices. We note that to investigate the contribution of an active galactic nucleus (AGN) in our templates, we also repeated the SED fitting for the stacked samples, excluding this time photometric points that are likely to be “polluted” by an AGN activity (i.e., $\lambda_{rest} < 60 \mu m$). The inferred $\langle U \rangle$ values are

very close to the values derived when considering the whole set of photometric points, in agreement with various studies that find a negligible effect of an AGN in the far-IR colors of a galaxy (e.g., Hatziminaoglou et al. 2010; Mullaney et al. 2012). We conclude that our templates should be representative for the bulk of MS galaxies, even for those that contain an average AGN contribution in the mid-IR.

8. DISCUSSION

It seems that the main physical parameter that drives the SFR of a normal galaxy is the gas fraction (or M_{gas}/M_*). Indeed, according to our analysis, at fixed stellar mass and redshift, there is a strong dependence of sSFR on M_{gas}/M_* , suggesting that the variations within the MS are due to variations in the f_{gas} of a galaxy. Interestingly, we find that within the MS, M_{gas}/M_* varies almost linearly with $\text{sSFR}/\text{sSFR}_{\text{MS}}$ (slope of ~ 0.9). It is important to recall that for the gas fractions inferred in this study we use the total gas mass of the galaxies. However, L_{IR} , and subsequently SFR, is known to strongly correlate with the HCN luminosity, which is a measure of dense gas (H_2 volume densities $> 10^4 \text{ cm}^{-3}$), for spirals, local (U)LIRGs, and QSOs, with an almost linear relation (Gao & Solomon 2004; Juneau et al. 2009). The inferred dependence of SFR on the total gas fraction, along with the fact that we do not observe substantial changes in the SFE, is indicative of a rather constant fraction of dense gas among MS galaxies. Alternatively, it suggests that the fluctuations of galaxies above and below MS are relatively long lasting, allowing the dense gas fraction to adjust. Indeed, given that the typical timescale for dense gas consumption is 10^8 yr (and given that it is only a fraction of the total gas), fluctuations have to last a similar or longer time. This is also the timescale required to allow integrated $U-V$ colors to change (Salmi et al. 2012). Furthermore, the fact that f_{gas} decreases with M_* implies that accretion does not keep up with SF and outflows at least at $z < 2$.

Another important implication of our analysis is that any attempt to constrain the evolution of f_{gas} (or M_{gas}/M_*) with cosmic time should be focused on narrow stellar mass ranges or take into account the f_{gas} dependence on both M_* and sSFR. Rescaling the f_{gas} estimates of the total stacked samples of $z \sim 1$ and $z \sim 2$ MS galaxies based on the derived trends between $M_{\text{gas}}/M_* - M_*$ and $M_{\text{gas}}/M_* - \text{sSFR}/\text{sSFR}_{\text{MS}}$, in Figure 17 we show the evolution of f_{gas} with redshift for galaxies of $\text{sSFR}/\text{sSFR}_{\text{MS}} = 1$ and $M_* = 5 \times 10^{10} M_{\odot}$. The evolution of f_{gas} is in excellent agreement with the observationally motivated tracks of M. Sargent et al. (2012, in preparation) that are built assuming $M_{\text{gas}} \propto \text{SFR}^{0.81}$ at all redshifts and an increase of sSFR as $(1+z)^{2.8}$ up to $z \sim 2.5$ followed by a flattening toward higher redshifts. We note that recently Magdis et al. (2012a) provided observational evidence for the plateau in the evolution of the f_{gas} at $z > 2$.

While it seems that there is no value of f_{gas} , stellar mass, or sSFR that could be regarded as representative for all MS galaxies at a given redshift, we find that MS galaxies appear to share very similar IR-SED shapes, with a characteristic $\langle U \rangle \propto L_{\text{IR}}/M_{\text{dust}}$ at each cosmic epoch. We find that MS galaxies tend to exhibit higher $L_{\text{IR}}/M_{\text{dust}}$ values as we move back in time, suggesting that there is evolution within the MS as a function of time toward warmer T_d . Nevertheless, we stress that high- z MS galaxies with ULIRG-like L_{IR} , while warmer than local, normal galaxies, are colder than local ULIRGs, in agreement with various studies that find an evolution in the T_d of ULIRGs (e.g., Hwang et al. 2010; Muzzin et al. 2010). On the other hand, the uniform SED

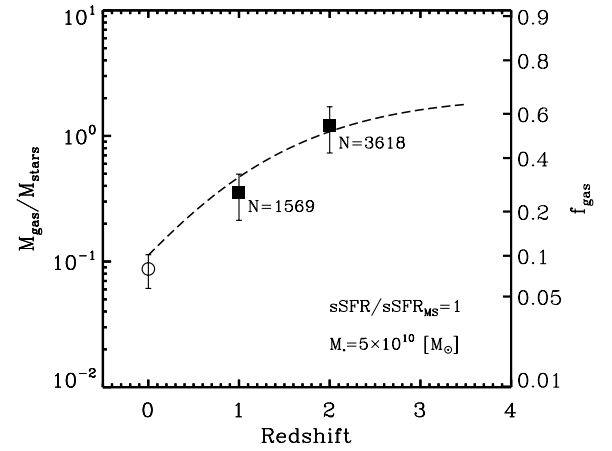


Figure 17. Evolution of M_{gas}/M_* with redshift of galaxies with $\text{sSFR}/\text{sSFR}_{\text{MS}} = 1$ and $M_* = 5 \times 10^{10} M_{\odot}$. The black squares correspond to M_{gas}/M_* of the total stacked samples of $z \sim 1$ and $z \sim 2$ main-sequence galaxies. The number next to the stacked points corresponds to the total number of objects that are included in the stack. The open circle at $z \sim 0$ corresponds to the mean f_{gas} of the Leroy et al. (2008) sample. All measurements have been corrected to refer to $M_* = 5 \times 10^{10} M_{\odot}$. The black dashed line depicts the evolution of M_{gas}/M_* with redshift for the case of $M_* = 5.0 \times 10^{10} M_{\odot}$, as implied by the cosmic evolution of sSFR (M. Sargent et al. 2012, in preparation).

shape of MS galaxies at a given redshift suggests that T_d does not change substantially with L_{IR} within the MS. Consequently, it is possible that the strong evolution of T_d with L_{IR} reported by several studies (e.g., Magdis et al. 2010a; Hwang et al. 2010) is a result of mixing MS galaxies at various redshifts, or MS and SB systems, the latter known to dominate the star-forming galaxy population at high luminosities (e.g., Rodighiero et al. 2011; Sargent et al. 2012). Although the limited number of starbursting galaxies in this study does not allow us to reach solid conclusions, based on Figure 15 (right) we can speculate that a similar, but less strong, evolution of $\langle U \rangle$, and therefore T_d , with look-back time is present for this population too (see Béthermin et al. 2012a for a possible implementation). A larger sample of galaxies with elevated sSFR with respect to the MS is necessary to extend this investigation.

We stress that the methodology presented in this study opens an alternative window for a systematic investigation of the gas properties for large samples of high- z galaxies, for which *Herschel* has provided a robust characterization of their SEDs. While this approach does not require CO emission line measurements and is free from the uncertain nature of α_{CO} , we stress that both techniques yield consistent results. However, it is important to recall the limitations of this methodology. The key assumption of this study is that the $\delta_{\text{GDR}}-Z$ relation observed in the local universe does not evolve substantially with time, implying that roughly half of the metals of high- z galaxies as well are locked into dust. Evidently, if the fraction is lower at higher redshifts, then the inferred M_{gas} would be underestimated. However, as we argued before, this is unlikely to be a strong effect; the opposite might actually be more plausibly expected. We also stress that the $\delta_{\text{GDR}}-Z$ relation is poorly constrained at the low-metallicity end ($Z < 8.0$), where it might even become strongly nonlinear. However, since the lowest metallicity considered in our study is ~ 8.3 (Figure 4, left, horizontal line), we do not expect to be affected by these uncertainties. Another possible caveat is also the assumed metallicities, for which we rely on empirical relations and measurements from the literature. For example, since the adopted relation to derive metallicities for the $z \sim 2$ sample has

been calibrated on UV-selected galaxies, one could imagine a possible bias toward underestimating the actual metallicity of galaxies in our sample (e.g., Onodera et al. 2010). If indeed the metallicity is underestimated, we would overestimate the true M_{gas} of the galaxies. However, we do not expect this effect to impact our main conclusions, given the flat shape of the observed stellar mass– Z relation (e.g., Erb et al. 2006). We also note that while stacking data for thousands of sources erases interesting details on individual sources, it also serves as a tool to average out the dispersion in the $M_{\text{gas}}-Z$ and $\delta_{\text{GDR}}-Z$ relations. However, this method is sensitive to M_{dust} measurements that could, in principle, be affected by systematic biases, up to a factor of ~ 3 if one allows for extreme variations in the properties of the dust grains. Also, we stress that using the templates presented in this study to infer the total L_{IR} of individual galaxies from a single detection in the Rayleigh–Jeans tail requires extreme caution due to the scatter in $\langle U \rangle$, which is not fully constrained at high z . Future, direct observations of individual sources in the Rayleigh–Jeans tail will guide this investigation and also address the physical origin of the scatter, which could be linked to the thickness both of the $M_{\text{gas}}-Z$ relation inside the MS and of the SF law. Finally, as indicated in Table 4, while the IR8 of the $z \sim 2$ stacked samples does not appear to vary with stellar mass (and hence SFR), there is evidence that it could increase with increasing distance to the MS, in agreement with Elbaz et al. (2011). Variations in IR8, $\langle U \rangle$, and possibly other physical parameters suggest that a single invariant SED for the whole MS should be treated as a good first-order approximation.

9. CONCLUSIONS

We have used a sample of nine normal galaxies at $z \sim 0.5$ and $z \sim 1.5$ and three high- z SMGs, all selected to benefit from low- J CO observations and high-quality far-IR photometry, to estimate their gas content and α_{CO} conversion factors. In addition, large stacked samples of >4000 mass-selected MS galaxies at $0.5 < z < 2.5$ were used to investigate the evolution of their M_{dust} and M_{gas} content over the past 10 billion years. The main findings and implications are summarized as follows:

1. For high- z normal galaxies, we derive an average α_{CO} value of 5.5 ± 0.4 , similar to that of local spirals, and ~ 5 times higher than that of local galaxies with comparable L_{IR} (i.e., (U)LIRGs). We also find that high- z MS galaxies are ~ 12 times less efficient at converting molecular gas to stars when compared to local SBs, with SFE $\sim 14 L_{\odot}/M_{\odot}$, corresponding to an average gas consumption timescale of 0.6 Gyr.
2. For MS galaxies at any redshift, we find a weak dependence of the dust-mass-weighted luminosity ($L_{\text{IR}}/M_{\text{dust}}$), or equally of the mean radiation field $\langle U \rangle$, on sSFR/sSFR_{MS} and M_{gas} , complemented by a mild evolution with cosmic time as $(1+z)^{1.15}$. Also, for $L_{\text{IR}} = L_{8-1000\mu\text{m}}$, we find an average scaling factor between $\langle U \rangle$ and $L_{\text{IR}}/M_{\text{dust}}$ of $P_0 \approx 125$.
3. We find clear trends of increasing $M_{\text{gas}}/M_{\text{ast}}$ (or equally of f_{gas}) with increasing sSFR/sSFR_{MS}, with a slope of $\xi_{\text{frac1}} \approx 0.9$ and decreasing $M_{\text{gas}}/M_{\text{ast}}$ with increasing M_{gas} with a slope of $\xi_{\text{frac2}} \approx -0.5$. Since at a given redshift f_{gas} varies with stellar mass and sSFR, any attempt to explore the evolution of f_{gas} with redshift should take into account these emerging trends.
4. All the above, taken together, lead to the conclusion that variation in the gas fraction (f_{gas}) is the driving physical

parameter responsible for the spread in the SFR– M_{gas} correlation traced by normal galaxies at any redshift, pointing toward a single, tight $L_{\text{IR}}-M_{\text{gas}}$ relation for MS galaxies.

5. We find that at a given redshift, MS galaxies seem to have uniform IR-SED shapes, as parameterized by the mean radiation field $\langle U \rangle \propto L_{\text{IR}}/M_{\text{dust}}$ of the DL07 models. Based on this result and on the derived evolution of $\langle U \rangle$ with redshift, we build and provide a set of redshift-dependent template SEDs of MS galaxies at various redshifts and show that the evolution of the SED of MS galaxies is primarily driven by the cosmic evolution of metallicity and is only marginally linked to the rise of average sSFR with redshift.

Together with the pilot study of Magdis et al. (2011), we have demonstrated for the first time the importance of studying the continuum SEDs of galaxies in order to place constraints on their gas content, through dust mass and metallicity estimates. We believe that this is a powerful technique: until we are in position to formally estimate α_{CO} for high- z galaxies using the resolving power of ALMA, it provides an alternative approach for the study of M_{gas} in galaxies throughout cosmic time. However, from our detailed investigation we can point out two important results regarding the derivation of dust masses that similar studies should keep in mind:

1. Dust mass estimates based on a single-temperature MBB model are, on average, a factor of ~ 2 lower compared to those derived using the physically motivated and more realistic models of Draine & Li (2007).
2. While rest-frame submillimeter data ($\lambda_{\text{rest}} > 200\mu\text{m}$) reduce the uncertainties in the inferred M_{dust} by a factor of two, excluding millimeter continuum data from the fit does not have an impact on the derived M_{dust} estimates of MS galaxies. On the other hand, it appears that in the absence of millimeter continuum data, M_{dust} estimates of starbursting systems can be grossly overestimated.

G.E.M. acknowledges support from the John Fell Oxford University Press (OUP) Research Fund and the University of Oxford and useful discussions with D.K.X., L.M., S.B., and F. Galliano. E. Daddi, M. Béthermin, and M. T. Sargent were supported by grants ERC- StG UPGAL 240039 and ANR-08-JCJC-0008. Support for this work was also provided by NASA through an award issued by JPL/Caltech. PACS has been developed by a consortium of institutes led by MPE (Germany) and including UVIE (Austria); KU Leuven, CSL, IMEC (Belgium); CEA, LAM (France); MPIA (Germany); INAF/IFSI/OAA/OAP/OAT, LENS, SISSA (Italy); and IAC (Spain). This development has been supported by the funding agencies BMVIT (Austria), ESA-PRODEX (Belgium), CEA/CNRS (France), DLR (Germany), ASI/INAF (Italy), and CICYT/MCYT (Spain). SPIRE has been developed by a consortium of institutes led by Cardiff University (UK) and including Univ. Lethbridge (Canada); NAOC (China); CEA, LAM (France); IFSI, Univ. Padua (Italy); IAC (Spain); Stockholm Observatory (Sweden); Imperial College London, RAL, UCL-MSSL, UKATC, Univ. Sussex (UK); and Caltech, JPL, NHSC, Univ. Colorado (USA). This development has been supported by national funding agencies: CSA (Canada); NAOC (China); CEA, CNRS, CNRS (France); ASI (Italy); MCINN (Spain); Stockholm Observatory (Sweden); STFC (UK); and NASA (USA). This paper used data from ESO program IDs 078.F-9028(A), 079.F-9500(A), 080.A-3023(A), and 081.F-9500(A).

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